DesCartes: A Continuum of Learning ${ }^{\circledR}$
Mathematics
Goal: The Real and Complex Number Systems

| Skills and Concepts to Develop (50\% Probability*) $<161$ | Skills and Concepts to Introduce (27\% Probability*) $161-170$ |
| :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships |
|  | - Completes a growing arithmetic pattern by naming missing members |
| Perform Operations | Perform Operations |
| - Adds 1-digit to multiple-digit number with regrouping <br> - Adds 1-digit to multiple-digit number with no regrouping <br> - Uses models to construct whole number addition facts with addends through 10 <br> - Uses models to calculate whole number sums through 99 <br> - Adds two 1-digit numbers with sums to 10 in horizontal format | - Adds 1-digit to multiple-digit number with regrouping <br> - Adds 2-digit numbers with no regrouping <br> - Solves real-world whole number addition problems with sums to 20 (result unknown) <br> - Subtracts two 1-digit numbers horizontally <br> - Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only) <br> - Subtracts two 1-digit numbers vertically <br> - Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is $0-12$ <br> - Subtracts a 2-digit number from a 2-digit number, with no regrouping <br> - Tells time to the nearest hour <br> - Tells time to the nearest half hour <br> - Uses a number line to construct addition facts with sums through 20 (whole numbers) <br> - Uses models to calculate whole number sums through 99 <br> - Adds two 1-digit numbers with sums to 10 in horizontal format <br> - Adds two 1-digit numbers with sums between 10 and 19 in horizontal format <br> - Adds two 1-digit numbers with sums between 10 and 19 in vertical format <br> - Adds multiple 1-digit numbers <br> - Uses strategies for addition facts (e.g., compatible numbers, counting on, doubles, neighbors, making tens) <br> - Adds 1 -digit to multiple-digit number with no regrouping |
| Extend and Use Properties | Extend and Use Properties |
| - Identifies whole numbers under 100 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 11 to 20 (e.g., 15 is fifteen, and vice versa) | - Identifies missing numbers in a series through 100 <br> - Writes whole numbers in standard and expanded form through the tens <br> - Orders whole numbers less than 10 <br> - Identifies whole numbers under 100 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 11 to 20 (e.g., 15 is fifteen, and vice versa) <br> - Counts 1 to 10 objects <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 |
| New Vocabulary: None | New Vocabulary: None |
| New Signs and Symbols: None | New Signs and Symbols: + addition, $=$ is equal to, $\times$ multiplication, subtraction, : used with time, variable |

DesCartes: A Continuum of Learning ${ }^{\circledR}$
Mathematics
Goal: The Real and Complex Number Systems


## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $<161$ | Skills and Concepts to Develop (50\% Probability*) 161-170 | Skills and Concepts to Introduce (27\% Probability*) 171-180 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
|  |  | - Subtracts a 1 -digit number from a 2 -digit number with no regrouping, vertically |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies whole numbers under 100 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 11 to 20 (e.g., 15 is fifteen, and vice versa) | - Identifies missing numbers in a series through 100 <br> - Writes whole numbers in standard and expanded form through the tens <br> - Orders whole numbers less than 10 <br> - Identifies whole numbers under 100 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 11 to 20 (e.g., 15 is fifteen, and vice versa) <br> - Counts 1 to 10 objects <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 | - Represents $1 / 2$ with a diagram or model <br> - Identifies the place value and value of each digit in whole numbers through the tens place <br> - Compares whole numbers through 999 <br> - Counts objects that are grouped into tens and ones <br> - Represents $1 / 4$ with a diagram or model <br> - Identifies whole numbers 100-999 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 21 to 100 <br> (e.g., 62 is sixty-two, and vice versa) <br> - Identifies one-half from a region or set <br> - Identifies the numeral and written name for whole numbers 101 to 999 <br> (e.g., 342 is three hundred forty-two, and vice versa) <br> - Identifies missing numbers in a series through 100 <br> - Counts by 2's to 100 <br> - Counts backwards from a given number (given number greater than 10) <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 <br> - Compares sets of objects and identifies which is equal to, more than, or less than the other ( 1 to 10 objects) |
| New Vocabulary: None | New Vocabulary: None | New Vocabulary: fact family, fourth, hundred, morning, thirds, thousand |
| New Signs and Symbols: None | New Signs and Symbols: + addition, $=$ is equal to, $\times$ multiplication, subtraction, : used with time, variable | New Signs and Symbols: ( ) order of operations, a.m., ¢ cent sign, \$ dollar sign, p.m., \| tally mark |

Goal: The Real and Complex Number Systems
Skills and concepts to Enhance (73\% Probability*)
$161-170$

Perform Operations

- Adds 1 -digit to multiple-digit number with regrouping
- Adds 2-digit numbers with no regrouping
- Solves real-world whole number addition problems with sums to 20 (result unknown)
- Subtracts two 1-digit numbers horizontally
- Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only)
- Subtracts two 1-digit numbers vertically
- Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12
- Subtracts a 2-digit number from a 2-digit number, with no regrouping
- Tells time to the nearest hour
- Tells time to the nearest half hour
- Uses a number line to construct addition facts with sums through 20 (whole numbers)
- Uses models to calculate whole number sums through 99
- Adds two 1-digit numbers with sums to 10 in horizontal format
- Adds two 1-digit numbers with sums between 10 and 19 in horizonta format
- Adds two 1-digit numbers with sums between 10 and 19 in vertical format
- Adds multiple 1-digit numbers
- Uses strategies for addition facts (e.g., compatible numbers, counting on, doubles, neighbors, making tens)
- Adds 1-digit to multiple-digit number with no regrouping

| Skills and Concepts to Develop (50\% Probability*) |
| :---: |
| $171-180$ |

- Completes a growing arithmetic pattern by naming missing members
- Completes a growing arithmetic pattern by naming missing member - Computes simple conversions among units of time (minutes in an hour, half hour, quarter hour)


## - Adds 3-digit numbers with no regrouping

- Subtracts a 2-digit number from a 2-digit number, with no regrouping
- Subtracts 2 - and/or 3-digit numbers with no regrouping
- Solves real-world whole number problems involving subtraction with numbers under 20
- Instantly recalls basic multiplication facts where one factor is 0-5 and the other factor is 0-12
- Multiplies basic facts to $10 \times 10$ vertically
- Adds 1-digit numbers with sums to 18 (with parentheses)
- Recognizes addition and subtraction fact families through 18
- Identifies the value of a collection of coins to $\$ 1.00$ (with pictures of coins)
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by "counting on" (with picture of money)
- Tells time to the nearest hour
- Tells time to the nearest half hour
- Tells time to the nearest 5 minutes
- Connects money with place value
- Determines the operation needed from a simple problem
- Uses a number line to construct addition facts with sums through 20 (whole numbers
- Uses models to calculate whole number sums through 999
- Uses strategies for addition facts (e.g., compatible numbers, counting on, doubles, neighbors, making tens)
- Adds two or three 2-digit number with regrouping
- Adds 1- and/or 2-digit numbers with sums under 100
- Adds 3-digit numbers, with regrouping, with sums under 1000
- Solves real-world whole number addition problems with sums to 20 (result unknown
- Solves real-world whole number addition problems with sums to 20 (start unknown)
- Solves real-world whole number addition problems with sums to 100 (result unknown)
- Subtracts a 1-digit number from a 2-digit number that is less than 20 (whole numbers only)


## Skills and Concepts to Introduce (27\% Probability*)

 181-19- Completes arithmetic growth patterns in number tables by identifying the missing elements
- Computes simple conversions among units of time (days, weeks)


## Perform Operations

- Performs mental subtraction with numbers under 1000
- Solves problems using the inverse relationship between addition and subtraction
- Uses counting by multiples for multiplication
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12
- Multiplies basic facts to $10 \times 10$ vertically
- Multiplies a 2-digit number by a 1-digit number with regrouping
- Multiplies a 2-digit number by a 2-digit number with no regrouping
- Solves word problems involving basic whole number multiplication facts to $10 \times 10$
- Uses manipulatives to divide a small set of objects into groups of equa size
- Uses sharing for division
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Models multiplication and division algorithms using arrays (whole numbers)
- Instantly recalls division facts with dividend and divisors less than 10
- Solves real-world whole number problems involving addition and subtraction
- Recognizes addition and subtraction fact families through 18 - Demonstrates an understanding of the inverse relationship between multiplication and division
- Adds decimals to the hundredths place (same number of digits) - Identifies the value of a collection of coins to $\$ 1.00$ (without picture of coins)
- Adds money with regrouping
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by "counting on" (with picture of money)
- Finds equivalent combinations of coins with the same value - Combines a collection of coins and identifies the correct notation
- Makes change to $\$ 1.00$ by "counting on" or subtracting
- Computes with dollars and cents up to and including $\$ 5.00$ and converts to decimals (addition/subtraction only)

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $161-170$ | Skills and Concepts to Develop (50\% Probability*) 171-180 |  |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
|  | - Subtracts a 1-digit number from a 2-digit number with no regrouping, vertically | - Computes 1 operation on addition or subtraction real-world problems involving money up to $\$ 5.00$ <br> - Identifies the correct time, given the words, and vice versa <br> - Determines elapsed clock time <br> - Determines elapsed time under 1 hour or to the hour <br> - Determines elapsed time involving whole hours, whole days, whole years <br> - Tells time to the nearest 5 minutes <br> - Determines the operation needed from a simple problem <br> - Identifies the number that is "1 less than" a given number <br> - Distinguishes between odd and even numbers <br> - Uses rounding to estimate answers to real-world problems involving addition of numbers less than 100 (whole numbers only) <br> - Instantly recalls basic addition facts with sums to 18 in a table <br> - Adds two or three 2-digit number with regrouping <br> - Adds 3-digit numbers, with regrouping, with sums under 1000 <br> - Performs mental computation with 2,3 , or 4 addends <br> - Adds two 3- and/or 4-digit numbers, with regrouping, with sums over 1000 <br> - Adds multiple-digit numbers, with regrouping, with sums over 1000 <br> - Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given <br> - Solves real-world whole number addition problems with sums to 100 (result unknown) <br> - Uses models to calculate differences through 100 (whole numbers) <br> - Instantly recalls basic subtraction facts with minuend less than 10 <br> - Subtracts a 2-digit number from a 2-digit number, with regrouping <br> - Uses strategies for sums and differences with 2-digit numbers (e.g., decomposing, compatible, compensation, partial sums, counting on) <br> - Subtracts 2-and/or 3-digit numbers with no regrouping <br> - Subtracts 3- or 4-digit numbers with regrouping <br> - Subtracts multiple-digit numbers with no regrouping <br> - Solves real-world whole number problems involving subtraction with numbers under 20 <br> - Solves real-world whole number problems involving subtraction with numbers 100 and under |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies missing numbers in a series through 100 <br> - Writes whole numbers in standard and expanded form through the tens <br> - Orders whole numbers less than 10 | - Represents $1 / 2$ with a diagram or model <br> - Identifies the place value and value of each digit in whole numbers through the tens place | - Counts objects that are grouped into tens and ones <br> - Compares and orders decimals to the hundredths place (same number of digits after decimal) |

## Explanatory Notes

 appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $161-170$ | Skills and Concepts to Develop (50\% Probability*) 171-180 | Skills and Concepts to Introduce (27\% Probability 181-190 |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies whole numbers under 100 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 11 to 20 (e.g., 15 is fifteen, and vice versa) <br> - Counts 1 to 10 objects <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 | - Compares whole numbers through 999 <br> - Counts objects that are grouped into tens and ones <br> - Represents $1 / 4$ with a diagram or model <br> - Identifies whole numbers 100-999 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 21 to 100 (e.g., 62 is sixty-two, and vice versa) <br> - Identifies one-half from a region or set <br> - Identifies the numeral and written name for whole numbers 101 to 999 (e.g., 342 is three hundred forty-two, and vice versa) <br> - Identifies missing numbers in a series through 100 <br> - Counts by 2's to 100 <br> - Counts backwards from a given number (given number greater than 10) <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 <br> - Compares sets of objects and identifies which is equal to, more than, or less than the other ( 1 to 10 objects) | - Identifies the numeral and written name for whole numbers 101 to 999 (e.g., 342 is three hundred forty-two, and vice versa) <br> - Identifies the numeral and written name for whole numbers to 1000 to 9999 (e.g., 3456 is three thousand, four hundred fifty-six, and vice versa) <br> - Identifies the numeral and written name for whole numbers 10,000 to 100,000 <br> - Compares whole numbers through 999 <br> - Compares whole numbers through 9999 <br> - Rounds 2- and 3- digit whole numbers to the nearest ten <br> - Rounds 3-digit whole numbers to the nearest hundred <br> - Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones = 34) <br> - Identifies the place value and value of each digit in whole numbers through the tens place <br> - Identifies the place value and value of each digit in whole numbers through the hundreds place <br> - Identifies the place value and value of each digit in whole numbers through the thousands <br> - Identifies the place value and value of each digit in whole numbers through the hundred thousands <br> - Represents $3 / 4$ with a diagram or model <br> - Identifies equal parts by using models <br> - Identifies $1 / 2$ from a region or set <br> - Identifies one-half from a region or set <br> - Identifies $1 / 4$ from a region or set <br> - Identifies $2 / 4,3 / 4$, or $4 / 4$ from a region or set <br> - Identifies $2 / 3$ or $3 / 3$ from a region or set <br> - Identifies tenths from a region or set <br> - Identifies eighths from a region or set <br> - Identifies a fraction (denominators other than 2, 3, 4, 8, 10) from a region or set |
| New Vocabulary: None | New Vocabulary: fact family, fourth, hundred, morning, thirds, thousand | New Vocabulary: changed, clock, closest, digit, fourths, gave, half past, how much time, hundreds, left, left over, million, nearest, noon, o'clock, one, pennies, quarter past, quarter to, row, ten thousand, unifix cubes, what time |
| New Signs and Symbols: + addition, $=$ is equal to, $\times$ multiplication, subtraction, : used with time, variable | New Signs and Symbols: ( ) order of operations, a.m., \& cent sign, \$ dollar sign, p.m., \| tally mark |  |
|  |  | New Signs and Symbols: $\}$ set notation, $\div$ division, long division symbol, : used with time, : used with time |

## Explanatory Notes


appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.
Skills and concepts to Enhance (73\% Probability*)
$171-180$

- Computes simple conversions among units of time (minutes in an hour, half hour, quarter hour)

| Skills and Concepts to Develop (50\% Probability*) |
| :---: | :---: |
| $181-190$ |

Ratios and Proportional Relationships

- Completes arithmetic
- Computes simple conversions among units of time (days, weeks)
Skills and Concepts to Introduce (27\% Probability*)
191-200 Ratios and Proportional Relationships
- Solves simple problems involving miles/kilometers per hour
- Converts between cups, pints, and quarts
- Solves problems involving basic percent concepts (e.g., $10 \%, 50 \%$, 100\%)
- Computes simple conversions among units of time (minutes, hours)
- Converts between cups and pints
- Writes the missing number in a proportion using basic facts

Perform Operations

- Adds 3-digit numbers with no regrouping
- Subtracts a 2 -digit number from a 2 -digit number, with no regrouping
- Subtracts 2-and/or 3-digit numbers with no regrouping
- Solves real-world whole number problems involving subtraction with numbers under 20
- Instantly recalls basic multiplication facts where one factor is $0-5$ and the other factor is $0-12$
- Multiplies basic facts to $10 \times 10$ vertically
- Adds 1 -digit numbers with sums to 18 (with parentheses)
- Recognizes addition and subtraction fact families through 18
- Identifies the value of a collection of coins to $\$ 1.00$ (with pictures of coins)
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by "counting on" (with picture of money)
- Tells time to the nearest hour
- Tells time to the nearest half hour
- Tells time to the nearest 5 minutes
- Connects money with place value
- Determines the operation needed from a simple problem
- Uses a number line to construct addition facts with sums through 20 (whole numbers)
- Uses models to calculate whole number sums through 999
- Uses strategies for addition facts (e.g., compatible numbers, counting on, doubles, neighbors, making tens)
- Adds two or three 2-digit number with regrouping
- Adds 1 - and/or 2-digit numbers with sums under 100
- Adds 3-digit numbers, with regrouping, with sums under 1000
- Solves real-world whole number addition problems with sums to 20 (result unknown)
- Solves real-world whole number addition problems with sums to 20 (start unknown)
Per
- Performs mental subtraction with numbers under 1000
- Solves problems using the inverse relationship between addition and subtraction
- Uses counting by multiples for multiplication
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12
- Multiplies basic facts to $10 \times 10$ vertically
- Multiplies a 2 -digit number by a 1 -digit number with regrouping
- Multiplies a 2 -digit number by a 2 -digit number with no regrouping
- Solves word problems involving basic whole number multiplication facts to $10 \times 10$
- Uses manipulatives to divide a small set of objects into groups of equal size
- Uses sharing for division
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Models multiplication and division algorithms using arrays (whole numbers)
- Instantly recalls division facts with dividend and divisors less than 10
- Solves real-world whole number problems involving addition and subtraction
- Recognizes addition and subtraction fact families through 18
- Demonstrates an understanding of the inverse relationship between multiplication and division
- Adds decimals to the hundredths place (same number of digits)
- Identifies the value of a collection of coins to $\$ 1.00$ (without picture of coins)
- Adds money with regrouping
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by "counting on" (with picture of money)
- Finds equivalent combinations of coins with the same value
- Determines elapsed time involving whole hours, whole days, whole years
- Multiplies a decimal by whole number
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with addition and subtraction (whole numbers only)
- Uses rounding to estimate answers to addition and subtraction problems (whole numbers only)
- Adds two 3-and/or 4-digit numbers, with regrouping, with sums over 1000
- Adds multiple-digit numbers, with regrouping, with sums over 1000 - Adds multiple-digit numbers with sums under 1000
- Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given
- Solves real-world whole number addition problems with sums to 20 (change unknown)
- Solves whole number addition word problems with sums over 1000 - Subtracts 1 -digit number from a 2 -digit number with regrouping
- Subtracts a 2 -digit number from a 2 -digit number, with regrouping - Uses strategies for sums and differences with 2-digit numbers (e.g., decomposing, compatible, compensation, partial sums, counting on)
- Subtracts a 2 -digit number from a 3 -digit number with a single regrouping
- Subtracts 3- or 4-digit numbers with regrouping
- Performs mental subtraction with numbers under 1000
- Subtracts multiple-digit numbers with no regrouping
- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves problems using the inverse relationship between addition and subtraction
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is $0-12$
- Multiplies a 2 - or 3 -digit number by a 1 -digit number with no regrouping

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) |
| :--- |
| $171-180$ |

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| Skills and concepts to Enhance (73\% Probability*) 171-180 | Skills and Concepts to Develop (50\% Probability*) 181-190 | to Introduce (27\% Probability*) 191-200 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
|  |  | - Makes change to $\$ 1.00$ by "counting on" or subtracting <br> - Solves real-world problems involving decimals (not money) using addition and subtraction <br> - Computes with dollars and cents up to and including \$5.00 and converts to decimals (addition/subtraction only) <br> - Computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only) <br> - Computes with dollars and cents up to and including $\$ 5.00$ and converts to decimals (multiplication/division) <br> - Computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division) <br> - Computes basic operations with units of weight/mass <br> - Identifies the correct time, given the words, and vice versa <br> - Determines elapsed clock time <br> - Tells time to the nearest quarter hour <br> - Tells time to the nearest 1 minute <br> - Solves simple problems involving elapsed time, with the conversion of hours <br> - Determines the operation needed from a simple problem <br> - Solves problems using tables <br> - Distinguishes between odd and even numbers <br> - Identifies numbers as composite |
| Extend and Use Prop | Extend and Use Properties | end and Use Properties |
| - Represents $1 / 2$ with a diagram or model <br> - Identifies the place value and value of each digit in whole numbers through the tens place <br> - Compares whole numbers through 999 <br> - Counts objects that are grouped into tens and ones <br> - Represents $1 / 4$ with a diagram or model <br> - Identifies whole numbers 100-999 using base-10 blocks <br> - Identifies the numerical and written name for whole numbers 21 to 100 (e.g., 62 is sixty-two, and vice versa) <br> - Identifies one-half from a region or set <br> - Identifies the numeral and written name for whole numbers 101 to 999 (e.g., 342 is three hundred forty-two, and vice versa) <br> - Identifies missing numbers in a series through 100 <br> - Counts by 2's to 100 <br> - Counts backwards from a given number (given number greater than 10) <br> - Recognizes and generates equivalent forms for the same number using physical models for whole numbers 11 to 20 | - Counts objects that are grouped into tens and ones <br> - Compares and orders decimals to the hundredths place (same number of digits after decimal) <br> - Identifies the numeral and written name for whole numbers 101 to 999 (e.g., 342 is three hundred forty-two, and vice versa) <br> - Identifies the numeral and written name for whole numbers to 1000 to 9999 (e.g., 3456 is three thousand, four hundred fifty-six, and vice versa) <br> - Identifies the numeral and written name for whole numbers 10,000 to 100,000 <br> - Compares whole numbers through 999 <br> - Compares whole numbers through 9999 <br> - Rounds 2-and 3- digit whole numbers to the nearest ten <br> - Rounds 3-digit whole numbers to the nearest hundred <br> - Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones = 34) <br> - Identifies the place value and value of each digit in whole numbers through the tens place | - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Identifies equivalent fractions using visual representations <br> - Matches numeric and visual representation of equivalent fractions <br> - Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph) <br> - Identifies whole numbers over 999 using base-10 blocks <br> - Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place <br> - Identifies the numeral and written name for whole numbers 10,000 to 100,000 <br> - Identifies the numeral and written name for whole numbers over 100,000 <br> - Compares whole numbers to 100 , using the symbols for 'less than', 'equal to', or 'greater than' (<, =, >) <br> - Compares whole numbers through the thousands using the symbols <, $>$, or = <br> - Rounds 2- and 3- digit whole numbers to the nearest ten |

## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics RIT Score Range:
181-190
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 171-180 | Skills and Concepts to Develop (50\% Probability*) $181-190$ | Skills and Concepts to Introduce (27\% Probability*) 191-200 |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Compares sets of objects and identifies which is equal to, more than, or less than the other ( 1 to 10 objects) | - Identifies the place value and value of each digit in whole numbers through the hundreds place <br> - Identifies the place value and value of each digit in whole numbers through the thousands <br> - Identifies the place value and value of each digit in whole numbers through the hundred thousands <br> - Represents $3 / 4$ with a diagram or model <br> - Identifies equal parts by using models <br> - Identifies $1 / 2$ from a region or set <br> - Identifies one-half from a region or set <br> - Identifies $1 / 4$ from a region or set <br> - Identifies $2 / 4,3 / 4$, or $4 / 4$ from a region or set <br> - Identifies $2 / 3$ or $3 / 3$ from a region or set <br> - Identifies tenths from a region or set <br> - Identifies eighths from a region or set <br> - Identifies a fraction (denominators other than 2, 3, 4, 8, 10) from a region or set | - Rounds 3-digit whole numbers to the nearest hundred <br> - Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones = 34) <br> - Identifies the place value and value of each digit in whole numbers through the thousands <br> - Identifies the place value and value of each digit in whole numbers through the hundred thousands <br> - Writes whole numbers in standard and expanded form through the hundreds <br> - Writes whole numbers in standard and expanded form through the thousands <br> - Represents $1 / 3$ with a diagram or model <br> - Represents fractions with denominators other than 2, 3, 4 with a diagram or model <br> - Identifies $1 / 4$ from a region or set <br> - Identifies $1 / 3$ from a region or set <br> - Identifies $2 / 3$ or $3 / 3$ from a region or set <br> - Identifies tenths from a region or set <br> - Identifies a fraction (denominators other than 2, 3, 4, 8, 10) from a region or set |
| New Vocabulary: fact family, fourth, hundred, morning, thirds, thousand | New Vocabulary: changed, clock, closest, digit, fourths, gave, half past, how much time, hundreds, left, left over, million, nearest, noon, o'clock, one, pennies, quarter past, quarter to, row, ten thousand, unifix cubes, what time | New Vocabulary: billion, composite number, decade, deposit, each, grid, hundred million, miles per hour, prime number, quintillion, standard numeral, trillion |
| New Signs and Symbols: ( ) order of operations, a.m., \& cent sign, \$ dollar sign, p.m., \| tally mark |  |  |
|  | what time <br> New Signs and Symbols: $\}$ set notation, $\div$ division, long division symbol, : used with time, : used with time | New Signs and Symbols: ( ) ordered pair, ${ }^{\circ} \mathrm{F}$ degrees Fahrenheit, g gram, > greater than, lb pound, < less than, min minute, mph miles per hour, \% percent, • point, R remainder |

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 181-190 | Skills and Concepts to Develop (50\% Probability*) 191-200 | Skills and Concepts to Introduce (27\% Probability*) 201-210 |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships | Ratios and Proportional Relationships |
| - Completes arithmetic growth patterns in number tables by identifying the missing elements <br> - Computes simple conversions among units of time (days, weeks) | - Solves simple problems involving miles/kilometers per hour <br> - Converts between cups, pints, and quarts <br> - Solves problems involving basic percent concepts (e.g., 10\%, 50\%, 100\%) <br> - Computes simple conversions among units of time (minutes, hours) <br> - Converts between cups and pints <br> - Writes the missing number in a proportion using basic facts | - Determines unit price <br> - Identifies the percent represented in a 2-D region <br> - Converts between inches and feet <br> - Solves simple problems involving measurement of length <br> - Estimates simple conversions involving length between the customary and metric system <br> - Converts between cups and pints <br> - Converts between cups, pints, and quarts <br> - Computes simple conversions among units of time (hours, days) <br> - Computes more difficult conversions among units of time <br> - Applies dimensional analysis to simple real-world problems (time) <br> - Solves simple problems involving miles per gallon <br> - Solves simple problems involving miles/kilometers per hour <br> - Writes the missing number in a proportion using basic facts |
| Perform Operations | Perform Operations | Perform Operations |
| - Performs mental subtraction with numbers under 1000 <br> - Solves problems using the inverse relationship between addition and subtraction <br> - Uses counting by multiples for multiplication <br> - Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12 <br> - Multiplies basic facts to $10 \times 10$ vertically <br> - Multiplies a 2-digit number by a 1-digit number with regrouping <br> - Multiplies a 2-digit number by a 2-digit number with no regrouping <br> - Solves word problems involving basic whole number multiplication facts to $10 \times 10$ <br> - Uses manipulatives to divide a small set of objects into groups of equal size <br> - Uses sharing for division <br> - Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction) <br> - Models multiplication and division algorithms using arrays (whole numbers) <br> - Instantly recalls division facts with dividend and divisors less than 10 <br> - Solves real-world whole number problems involving addition and subtraction <br> - Recognizes addition and subtraction fact families through 18 <br> - Demonstrates an understanding of the inverse relationship between multiplication and division | - Determines elapsed time involving whole hours, whole days, whole years <br> - Multiplies a decimal by whole number <br> - Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with addition and subtraction (whole numbers only) <br> - Uses rounding to estimate answers to addition and subtraction problems (whole numbers only) <br> - Adds two 3- and/or 4-digit numbers, with regrouping, with sums over 1000 <br> - Adds multiple-digit numbers, with regrouping, with sums over 1000 <br> - Adds multiple-digit numbers with sums under 1000 <br> - Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given <br> - Solves real-world whole number addition problems with sums to 20 (change unknown) <br> - Solves whole number addition word problems with sums over 1000 <br> - Subtracts 1-digit number from a 2-digit number with regrouping <br> - Subtracts a 2-digit number from a 2-digit number, with regrouping <br> - Uses strategies for sums and differences with 2-digit numbers (e.g., decomposing, compatible, compensation, partial sums, counting on) <br> - Subtracts a 2-digit number from a 3-digit number with a single regrouping <br> - Subtracts 3- or 4-digit numbers with regrouping <br> - Performs mental subtraction with numbers under 1000 | - Multiplies a fraction by a fraction without reducing to simplest form (simple problem) <br> - Divides a 3-digit number by a 1-digit number with no remainder <br> - Divides a 4-digit number by a 1-digit number with no remainder <br> - Divides a 3-digit number by a multiple of 10 <br> - Divides a 4-digit number by a 2-digit number <br> - Solves word problems with whole number division facts with dividend and divisors less than 11 <br> - Solves simple word problems involving whole number division with remainder (e.g., 1-step, 1-digit divisor) <br> - Performs mental computation with division <br> - Solves whole number word problems with division over $10 \times 10$ <br> - Determines the remainder in a real-world problem (whole numbers) <br> - Uses division for multiple-step real-world problems (whole numbers) <br> - Solves real-world problems involving 2-step multiple operations, whole numbers only <br> - Adds fractions with like denominators without reducing <br> - Adds whole numbers and fractions <br> - Uses models to add and subtract fractions and connect the actions to algorithms <br> - Subtracts fractions with like denominators without reducing <br> - Subtracts mixed fractions with like denominators with no regrouping <br> - Solves real-world 1-step problems involving addition and subtraction of fractions with like denominators |

## Explanatory Notes


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| Skills and concepts to Enhance (73\% Probability*) |  |  |
| :--- | :---: | :---: |
| 181-190 |  |  |

- Adds decimals to the hundredths place (same number of digits)
- Identifies the value of a collection of coins to $\$ 1.00$ (without picture of coins)
- Adds money with regrouping
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by
"counting on" (with picture of money)
- Finds equivalent combinations of coins with the same value
- Combines a collection of coins and identifies the correct notation
- Makes change to $\$ 1.00$ by "counting on" or subtracting
- Computes with dollars and cents up to and including $\$ 5.00$ and converts to decimals (addition/subtraction only)
- Computes 1 operation on addition or subtraction real-world problems involving money up to $\$ 5.00$
- Identifies the correct time, given the words, and vice versa
- Determines elapsed clock time
- Determines elapsed time under 1 hour or to the hour
- Determines elapsed time involving whole hours, whole days, whole years
- Tells time to the nearest 5 minutes
- Determines the operation needed from a simple problem
- Identifies the number that is "1 less than" a given number
- Distinguishes between odd and even numbers
- Uses rounding to estimate answers to real-world problems involving addition of numbers less than 100 (whole numbers only)
- Instantly recalls basic addition facts with sums to 18 in a table
- Adds two or three 2 -digit number with regrouping
- Adds 3 -digit numbers, with regrouping, with sums under 1000
- Performs mental computation with 2, 3, or 4 addends
- Adds two 3 - and/or 4-digit numbers, with regrouping, with sums over 1000
- Adds multiple-digit numbers, with regrouping, with sums over 1000 - Solves real-world whole number addition problems with sums to 20 (result unknown) - with extraneous information given
- Solves real-world whole number addition problems with sums to 100 (result unknown)
- Uses models to calculate differences through 100 (whole numbers) - Instantly recalls basic subtraction facts with minuend less than 10
- Subtracts a 2 -digit number from a 2 -digit number, with regrouping
- Uses strategies for sums and differences with 2-digit numbers (e.g., decomposing, compatible, compensation, partial sums, counting on)
Skills and Concepts to Develop (50\% Probability*)

Perform Operations
Subtracts multiple-digit numbers with no regrouping

- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves problems using the inverse relationship between addition and subtraction
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is 0-12
- Multiplies a 2 - or 3 -digit number by a 1 -digit number with no regrouping - Multiplies a 2 -digit number by a 1 -digit number with regrouping
- Multiplies a 3 - or 4 -digit number by a 1 -digit number
- Multiplies a 2-digit number by a 2-digit number with no regrouping
- Performs mental computation with multiplication
- Solves word problems involving basic whole number multiplication facts to $10 \times 10$
- Solves word problems involving whole number multiplication with numbers greater than $10 \times 10$
- Uses manipulatives to divide a small set of objects into groups of equal size
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Instantly recalls division facts with dividend and divisors less than 10 - Instantly recalls division facts with dividend and divisors less than 13 - Divides a 2 -digit number by a 1 -digit number with no remainder
- Solves word problems with whole number division facts with dividend and divisors less than 11
- Solves simple word problems involving whole number division with remainder (e.g., 1 -step, 1 -digit divisor)
- Uses models to add and subtract fractions and connect the actions to algorithms
- Subtracts fractions with like denominators without reducing
- Solves real-world 1 -step problems involving addition and subtraction of fractions with like denominators
- Solves real-world 1 -step problems involving multiplication or division of a whole number by a fraction
- Adds decimals to the hundredths place (same number of digits)
- Adds decimals to the hundredths place in vertical format (not same number of digits)
- Adds decimals to the thousandths place vertically with and without regrouping
- Identifies the value of a collection of coins to $\$ 1.00$ (without picture of coins)
Skills and Concepts to Introduce (27\% Probability*)
201-210
- Adds decimals to the thousandths place horizontally with and without regrouping
- Subtracts decimals to the hundredths place (same number of digits) with regrouping
- Subtracts decimals to the thousandths place, vertically, with and without regrouping
- Subtracts decimals through the hundred-thousandths place, vertically
- Computes the value of multiple bills and coins (addition/subtraction only)
- Multiplies a decimal by whole number
- Divides decimal by a whole number
- Computes with dollars and cents up to and including $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes addition and subtraction on multiple-step real-world problems involving money
- Computes money problems with multiple operations (addition/ subtraction only)
- Computes addition, subtraction, multiplication, and division on multiple step, real-world problems involving money
- Solves real-world problems involving addition and subtraction of integers
- Solves problems involving measurement of time
- Solves simple problems involving elapsed time, with the conversion of hours
- Solves problems using tables
- Writes a terminating decimal as a fraction or mixed number
- Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only)
- Uses rounding to estimate answers to addition and subtraction problems (whole numbers only)
- Adds multiple-digit numbers, with regrouping, with sums over 1000
- Adds multiple-digit numbers with sums under 1000
- Performs mental computation with more than 4 addends
- Subtracts 3- or 4-digit numbers with regrouping
- Subtracts numbers with 5 digits or more with regrouping
- Solves real-world whole number problems involving subtraction with numbers 100 and under (analysis)
- Solves problems using the inverse relationship between addition and subtraction

Explanatory Notes


DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) |
| :--- |
| 181-190 |
| Perform Operations |
| - Subtracts 2- and/or 3-digit numbers with no regrouping |
| - Subtracts 3- or 4-digit numbers with regrouping |
| - Subtracts multiple-digit numbers with no regrouping |
| - Solves real-world whole number problems involving subtraction with |
| numbers under 20 |
| - Solves real-world whole number problems involving subtraction with |
| numbers 100 and under |

Extend and Use Properties

- Counts objects that are grouped into tens and ones
- Compares and orders decimals to the hundredths place (same number of digits after decimal)
- Identifies the numeral and written name for whole numbers 101 to 999 (e.g., 342 is three hundred forty-two, and vice versa)
- Identifies the numeral and written name for whole numbers to 1000 to 9999 (e.g., 3456 is three thousand, four hundred fifty-six, and vice versa) - Identifies the numeral and written name for whole numbers 10,000 to 100,000
- Compares whole numbers through 999

Skills and Concepts to Develop (50\% Probability*)
Perform Operations

## - Adds money with regrouping

- Identifies the value of a collection of coins and bills to $\$ 10.00$ by "counting on" (without picture of money)
- Finds equivalent combinations of coins with the same value
- Subtracts decimals to the hundredths place (same number of digits) with regrouping
- Subtracts decimals to the thousandths place, vertically, with and without regrouping
- Makes change to $\$ 1.00$ by "counting on" or subtracting
- Solves real-world problems involving decimals (not money) using addition and subtraction
- Computes with dollars and cents up to and including \$5.00 and converts to decimals (addition/subtraction only)
- Computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only)
- Computes with dollars and cents up to and including \$5.00 and converts to decimals (multiplication/division)
- Computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division)
- Computes basic operations with units of weight/mass
- Identifies the correct time, given the words, and vice versa
- Determines elapsed clock time
- Tells time to the nearest quarter hour
- Tells time to the nearest 1 minute
- Solves simple problems involving elapsed time, with the conversion of hours
- Determines the operation needed from a simple problem
- Solves problems using tables
- Distinguishes between odd and even numbers
- Identifies numbers as composite


## Extend and Use Properties

- Explains different interpretations of fractions (e.g., parts of a whole parts of a set, and division of whole numbers by whole numbers) - Identifies equivalent fractions using visual representations - Matches numeric and visual representation of equivalent fractions - Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph)
- Identifies whole numbers over 999 using base-10 blocks
- Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place

| Skills and Concepts to Introduce (27\% Probability*) |
| :---: |
| 201-210 |

- Instantly recalls basic multiplication and division facts in a table
- Multiplies a 2-digit number by a 1-digit number with regrouping
- Multiplies a 3- or 4-digit number by a 1-digit number
- Multiplies multiple 1-digit numbers
- Multiplies a 2-digit number by a 2-digit number with regrouping
- Multiplies a 3-digit number by a 2-digit number with regrouping
- Performs mental computation with multiplication
- Multiplies a 2- or 3-digit number by multiples of 10 or 100
- Multiplies a 3-digit number by a 3-digit number
- Solves word problems involving whole number multiplication with numbers greater than $10 \times 10$
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Instantly recalls division facts with dividend and divisors less than 13
- Divides a 2-digit number by a 1-digit number with no remainder
- Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 181-190 | Skills and Concepts to Develop (50\% Probability*) 191-200 | Skills and Concepts to Introduce (27\% Probability*) 201-210 |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |

- Compares whole numbers through 9999
- Rounds 2-and 3-digit whole numbers to the nearest ten
- Rounds 3-digit whole numbers to the nearest hundred
- Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones =34)
- Identifies the place value and value of each digit in whole numbers through the tens place
- Identifies the place value and value of each digit in whole numbers through the hundreds place
- Identifies the place value and value of each digit in whole numbers through the thousands
- Identifies the place value and value of each digit in whole numbers through the hundred thousands
- Represents $3 / 4$ with a diagram or model
- Identifies equal parts by using models
- Identifies $1 / 2$ from a region or set
- Identifies one-half from a region or set
- Identifies $1 / 4$ from a region or set
- Identifies $2 / 4,3 / 4$, or $4 / 4$ from a region or set
- Identifies $2 / 3$ or $3 / 3$ from a region or set
- Identifies tenths from a region or set
- Identifies eighths from a region or set
- Identifies a fraction (denominators other than 2, 3, 4, 8, 10) from a region or set
- Identifies the numeral and written name for whole numbers 10,000 to 100,000
- Identifies the numeral and written name for whole numbers over

100,000

- Compares whole numbers to 100 , using the symbols for 'less than', 'equal to', or 'greater than' (<, =, >)
- Compares whole numbers through the thousands using the symbols < $>$, or =
- Rounds 2-and 3-digit whole numbers to the nearest ten
- Rounds 3-digit whole numbers to the nearest hundred
- Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones $=34$ )
- Identifies the place value and value of each digit in whole numbers through the thousands
- Identifies the place value and value of each digit in whole numbers through the hundred thousands
- Writes whole numbers in standard and expanded form through the hundreds
- Writes whole numbers in standard and expanded form through the thousands
- Represents $1 / 3$ with a diagram or model
- Represents fractions with denominators other than 2, 3, 4 with a diagram or model
- Identifies $1 / 4$ from a region or set
- Identifies $1 / 3$ from a region or set
- Identifies $2 / 3$ or $3 / 3$ from a region or set
- Identifies tenths from a region or set
- Identifies a fraction (denominators other than 2, 3, 4, 8, 10) from a region or set
- Rounds wholes numbers to the nearest billion
- Compares integers on a number line
- Explains the rules for rounding
- Writes equivalent forms of whole numbers using place value (e.g., 54 $=4$ tens and 14 ones)
- Identifies the place value and value of each digit in whole numbers through the billions
- Writes whole numbers in standard and expanded form through the hundred thousands
- Applies base ten place value concepts with whole numbers to solve problems
- Writes whole numbers using place value terms and vice versa
- Identifies halves of a region using nonadjacent parts
- Identifies equivalent fractions using visual representations
-Expresses "1" in many different ways (e.g., 3/3, 4/4)
- Converts a basic fractional numeral to lowest terms (e.g., halves, thirds, quarters)
- Writes mixed numbers as improper fractions and improper fractions as mixed numbers
- Compares fractions (e.g., common denominator, 1 in the numerator, denominator is $2,3,4,6,8,10$ )
- Identifies whole numbers over 999 using base-10 blocks
- Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place
- Orders fractions on a number line
- Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers)
- Identifies a decimal on a number line to the tenths place
- Rounds decimals to the nearest whole number
- Graphs ordered pairs in the first quadrant
- Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph)
- Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system
- Determines the distance between points, following grid lines, in the first quadrant on a coordinate graph (as in city blocks)
- Locates the origin on a coordinate grid


## DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 181-190 | Skills and Concepts to Develop (50\% Probability*) 191-200 | Skills and Concepts to Introduce (27\% Probability*) 201-210 |
| :---: | :---: | :---: |
| New Vocabulary: changed, clock, closest, digit, fourths, gave, half past, how much time, hundreds, left, left over, million, nearest, noon, o'clock, one, pennies, quarter past, quarter to, row, ten thousand, unifix cubes, what time | New Vocabulary: billion, composite number, decade, deposit, each, grid, hundred million, miles per hour, prime number, quintillion, standard numeral, trillion | New Vocabulary: biggest, coordinate, coordinate point, expanded numeral, larger, miles per gallon, origin |
|  |  | New Signs and Symbols: ft feet, in. inch, mpg miles per gallon, - negative number |
| New Signs and Symbols: $\}$ set notation, $\div$ division, long division symbol, : used with time, : used with time | New Signs and Symbols: ( ) ordered pair, ${ }^{\circ}$ F degrees Fahrenheit, g gram, > greater than, lb pound, < less than, min minute, mph miles per hour, \% percent, • point, R remainder |  |

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems
Skills and concepts to Enhance (73\% Probability*)
$191-200$

| Skills and Concepts to Develop (50\% Probability*) <br> $201-210$ |  |  |
| :--- | :--- | :--- |
|  | Ratios and Proportional Relationships | R |
| . Dermine unit price | . |  |

## - Determines unit price

- Identifies the percent represented in a 2-D region
- Converts between inches and feet
- Solves simple problems involving measurement of length
- Estimates simple conversions involving length between the customary and metric system
- Converts between cups and pints
- Converts between cups, pints, and quarts
- Computes simple conversions among units of time (hours, days)
- Computes more difficult conversions among units of time
- Applies dimensional analysis to simple real-world problems (time)
- Solves simple problems involving miles per gallon
- Solves simple problems involving miles/kilometers per hour
- Writes the missing number in a proportion using basic facts
- Solves problems involving equivalent fractions
- Solves 1 -step problems involving proportions
- Calculates basic percents of a number (e.g., 10\%, 20\%, 25\%, 50\%, 100\%)
- Converts between inches and fee
- Converts between inches, feet, and yards
- Solves simple problems involving measurement of length
- Converts between cups, pints, quarts, and gallons
- Apply dimensional analysis to simple real-world problems (capacity)
- Computes more difficult conversions among units of time
- Applies dimensional analysis to simple real-world problems (time)
- Solves simple problems involving miles per gallon
- Determines unit price
- Solves problems involving rates
- Writes a basic percent as a fraction and vice versa (e.g., 10\%, 25\%, 50\%, 100\%)
- Expresses a percent as a fraction with 100 as the denominator and vice versa
- Recognizes and writes proportions
- Identifies the percent represented in a 2-D region
Perform Operations $\quad$ Perform Operations
- Subtracts mixed fractions with like denominators with no regrouping - Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Uses rounding to estimate answers to difficult multiplication and division problems (whole numbers only)
- Subtracts numbers with 5 digits or more with regrouping - Instantly recalls basic multiplication and division facts in a table - Multiplies a 2-digit number by a 2-digit number with regrouping - Multiplies a 3-digit number by a 2-digit number with regrouping - Performs mental computation with multiplication
- Uses multiplication strategies to explain computation (e.g., doubles, 9 patterns, decomposing, partial products)

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

decomposing, compatible, compensation, partial sums, counting on)

- Subtracts a 2 -digit number from a 3 -digit number with a single regrouping
- Subtracts 3- or 4-digit numbers with regrouping
- Performs mental subtraction with numbers under 1000
- Subtracts multiple-digit numbers with no regrouping
- Solves real-world whole number problems involving subtraction with numbers 100 and under
- Solves problems using the inverse relationship between addition and subtraction
- Instantly recalls basic multiplication facts where one factor is 6-12 and the other factor is $0-12$
- Multiplies a 2 - or 3 -digit number by a 1 -digit number with no regrouping
- Multiplies a 2 -digit number by a 1 -digit number with regrouping
- Multiplies a 3 - or 4 -digit number by a 1 -digit number
- Multiplies a 2 -digit number by a 2-digit number with no regrouping
- Performs mental computation with multiplication
- Solves word problems involving basic whole number multiplication facts to $10 \times 10$
- Solves word problems involving whole number multiplication with numbers greater than $10 \times 10$
- Uses manipulatives to divide a small set of objects into groups of equal size
- Models whole number multiplication and division algorithms (e.g., shows multiplication as repeated addition and division as repeated subtraction)
- Instantly recalls division facts with dividend and divisors less than 10 - Instantly recalls division facts with dividend and divisors less than 13
- Divides a 2 -digit number by a 1 -digit number with no remainder
- Solves word problems with whole number division facts with dividend and divisors less than 11
- Solves simple word problems involving whole number division with remainder (e.g., 1 -step, 1 -digit divisor)
- Uses models to add and subtract fractions and connect the actions to algorithms
- Subtracts fractions with like denominators without reducing
- Solves real-world 1 -step problems involving addition and subtraction of fractions with like denominators
- Solves real-world 1 -step problems involving multiplication or division of a whole number by a fraction

- Uses models to add and subtract fractions and connect the actions to - Uses mod
- Subtracts fractions with like denominators without reducing
- Subtracts mixed fractions with like denominators with no regrouping
- Solves real-world 1 -step problems involving addition and subtraction of fractions with like denominators
- Adds decimals to the thousandths place horizontally with and without regrouping
- Subtracts decimals to the hundredths place (same number of digits) with regrouping
- Subtracts decimals to the thousandths place, vertically, with and without regrouping
- Subtracts decimals through the hundred-thousandths place, vertically
- Computes the value of multiple bills and coins (addition/subtraction only)
- Multiplies a decimal by whole number
- Divides decimal by a whole number
- Computes with dollars and cents up to and including $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes addition and subtraction on multiple-step real-world problems involving money
- Computes money problems with multiple operations (addition/ subtraction only)
- Computes addition, subtraction, multiplication, and division on multiplestep, real-world problems involving money
- Solves real-world problems involving addition and subtraction of integers
- Solves problems involving measurement of time
- Solves simple problems involving elapsed time, with the conversion of hours
- Solves problems using tables
- Writes a terminating decimal as a fraction or mixed number
- Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only)
- Uses rounding to estimate answers to addition and subtraction problems (whole numbers only)
- Adds multiple-digit numbers, with regrouping, with sums over 1000
- Adds multiple-digit numbers with sums under 1000
- Performs mental computation with more than 4 addends


## - Multiplies a 3-digit number by a 3-digit numbe

## - Multiplies a 4- or more digit number by multiples of 100 or 1000

- Multiplies multiple-digit numbers
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder
- Performs mental computation with division
- Divides a 4-digit number by a 1-digit number with no remainder
- Divides a 3-digit number by a 2-digit number
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves whole number word problems with division over $10 \times 10$
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves real-world multiple-step problems involving whole numbers
- Demonstrates an understanding of the inverse relationship between addition and subtraction
- Adds fractions with like denominators without reducing
- Adds fractions with like denominators with reducing or converting to a mixed fraction
- Adds fractions with unlike denominators without reducing
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)
- Subtracts fractions with unlike denominators without reducing
- Subtracts mixed fractions with unlike denominators with no regrouping - Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number
- Solves 1 -step real-world problems involving fractions with multiplication and division
- Adds decimals to the hundredths place in horizontal format (not same number of digits)

Goal: The Real and Complex Number Systems
Skills and concepts to Enhance (73\% Probability*)
$191-200$

- Adds decimals to the hundredths place in vertical format (not same number of digits)
- Adds decimals to the thousandths place vertically with and without regrouping
- Identifies the value of a collection of coins to $\$ 1.00$ (without picture of coins)
- Adds money with regrouping
- Identifies the value of a collection of coins and bills to $\$ 10.00$ by
"counting on" (without picture of money)
- Finds equivalent combinations of coins with the same value
- Subtracts decimals to the hundredths place (same number of digits) with regrouping
- Subtracts decimals to the thousandths place, vertically, with and without regrouping
- Makes change to $\$ 1.00$ by "counting on" or subtracting
- Solves real-world problems involving decimals (not money) using addition and subtraction
- Computes with dollars and cents up to and including \$5.00 and converts to decimals (addition/subtraction only)
- Computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only)
- Computes with dollars and cents up to and including \$5.00 and converts to decimals (multiplication/division)
- Computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division)
- Computes basic operations with units of weight/mass
- Identifies the correct time, given the words, and vice versa
- Determines elapsed clock time
- Tells time to the nearest quarter hour
- Tells time to the nearest 1 minute
- Solves simple problems involving elapsed time, with the conversion of hours
- Determines the operation needed from a simple problem
- Solves problems using tables
- Distinguishes between odd and even numbers
- Identifies numbers as composite


## Skills and Concepts to Develop (50\% Probability*)

Perform Operations

- Subtracts 3- or 4-digit numbers with regrouping
- Subtracts numbers with 5 digits or more with regrouping
- Solves real-world whole number problems involving subtraction with numbers 100 and under (analysis)
- Solves problems using the inverse relationship between addition and subtraction
- Instantly recalls basic multiplication and division facts in a table
- Multiplies a 2-digit number by a 1-digit number with regrouping
- Multiplies a 3- or 4-digit number by a 1-digit number
- Multiplies multiple 1-digit numbers
- Multiplies a 2-digit number by a 2-digit number with regrouping
- Multiplies a 3-digit number by a 2-digit number with regrouping
- Performs mental computation with multiplication
- Multiplies a 2- or 3-digit number by multiples of 10 or 100
- Multiplies a 3-digit number by a 3-digit number
- Solves word problems involving whole number multiplication with numbers greater than $10 \times 10$
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Instantly recalls division facts with dividend and divisors less than 13 - Divides a 2-digit number by a 1-digit number with no remainder - Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder

| Skills and Concepts to Introduce (27\% Probability*) |
| :--- | :--- |
| 211-220 |

- Adds decimals to the thousandths place horizontally with and without regrouping
- Adds decimals through the hundred-thousandths place
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Computes the value of multiple bills and coins (addition/subtraction only)
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only)
- Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
- Multiplies a decimal by a decimal (factors to hundredths)
- Divides decimal by a whole number
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division)
- Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes addition and subtraction on multiple-step real-world problems involving money
- Computes addition, subtraction, multiplication, and division on multiplestep, real-world problems involving money
- Adds integers with like signs
- Uses models to add and subtract integers and connect the actions to algorithms
- Solves real-world problems involving addition and subtraction of integers
- Multiplies integers with unlike signs
- Divides integers with unlike signs
- Divides integers with like signs
- Demonstrates an understanding that division by 0 is undefined
- Solves difficult problems involving elapsed time, with the conversion of hours
- Selects and uses the appropriate units depending on degree of accuracy required to solve problems
- Expresses a simple fraction as a decimal
- Writes a simple mixed fraction as a decimal and vice versa
- Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10
- Expresses a percent as a decimal and vice versa
- Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 191-200 | Skills and Concepts to Develop (50\% Probability*) 201-210 | Skills and Concepts to Introduce (27\% Probability*) 211-220 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
|  |  | - Determines factors of whole numbers <br> - Identifies numbers as prime <br> - Identifies common factors of two or more numbers <br> - Identifies the greatest common factor of whole numbers |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Identifies equivalent fractions using visual representations <br> - Matches numeric and visual representation of equivalent fractions <br> - Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph) <br> - Identifies whole numbers over 999 using base-10 blocks <br> - Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place <br> - Identifies the numeral and written name for whole numbers 10,000 to 100,000 <br> - Identifies the numeral and written name for whole numbers over 100,000 <br> - Compares whole numbers to 100 , using the symbols for 'less than', 'equal to', or 'greater than' (<, =, >) <br> - Compares whole numbers through the thousands using the symbols <, >, or = <br> - Rounds 2-and 3-digit whole numbers to the nearest ten <br> - Rounds 3-digit whole numbers to the nearest hundred <br> - Identifies whole numbers under 100 given place value terms (e.g., 3 tens and 4 ones = 34) <br> - Identifies the place value and value of each digit in whole numbers through the thousands <br> - Identifies the place value and value of each digit in whole numbers through the hundred thousands <br> - Writes whole numbers in standard and expanded form through the hundreds <br> - Writes whole numbers in standard and expanded form through the thousands <br> - Represents $1 / 3$ with a diagram or model <br> - Represents fractions with denominators other than 2, 3, 4 with a diagram or model <br> - Identifies $1 / 4$ from a region or set <br> - Identifies $1 / 3$ from a region or set <br> - Identifies $2 / 3$ or $3 / 3$ from a region or set <br> - Identifies tenths from a region or set | - Identifies the numeral and written name for whole numbers over 100,000 <br> - Compares whole numbers through the billions using the symbols <, >, or = <br> - Orders whole numbers a million or greater using < or > symbols <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand <br> - Rounds whole numbers to the nearest hundred thousand <br> - Rounds wholes numbers to the nearest billion <br> - Compares integers on a number line <br> - Explains the rules for rounding <br> - Writes equivalent forms of whole numbers using place value (e.g., 54 $=4$ tens and 14 ones) <br> - Identifies the place value and value of each digit in whole numbers through the billions <br> - Writes whole numbers in standard and expanded form through the hundred thousands <br> - Applies base ten place value concepts with whole numbers to solve problems <br> - Writes whole numbers using place value terms and vice versa <br> - Identifies halves of a region using nonadjacent parts <br> - Identifies equivalent fractions using visual representations <br> - Expresses "1" in many different ways (e.g., 3/3, 4/4) <br> - Converts a basic fractional numeral to lowest terms (e.g., halves, thirds, quarters) <br> - Writes mixed numbers as improper fractions and improper fractions as mixed numbers <br> - Compares fractions (e.g., common denominator, 1 in the numerator, denominator is $2,3,4,6,8,10$ ) <br> - Identifies whole numbers over 999 using base-10 blocks <br> - Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place <br> - Orders fractions on a number line | - Converts fractions to lowest terms <br> - Predicts the relative size of the answer when computing with 10 's, 100's, 1000's <br> - Predicts the relative size of the answer when multiplying whole numbers <br> - Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system <br> - Locates the origin on a coordinate grid <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten thousand <br> - Rounds wholes numbers to the nearest billion <br> - Writes whole numbers in standard and expanded form through the hundred thousands <br> - Identifies equivalent fractions using visual representations <br> - Identifies a fractions in lowest terms from a region or set <br> - Identifies eighths, reduced to lowest terms, from a region or set <br> - Determines simple equivalent fractions using multiples <br> - Writes mixed numbers as improper fractions and improper fractions as mixed numbers <br> - Compares fractions on a number line <br> - Compares fractions greater than or less than a given fraction using visual representations <br> - Compares fractions and mixed numbers <br> - Compares fractions and mixed numbers using symbols <br> - Orders fractions on a number line <br> - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Represents a decimal to the hundredths place (e.g., three hundredths = 0.03) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest whole number <br> - Rounds decimals to the nearest tenth <br> - Applies base ten place value concepts to solve problems using decimals |

Explanatory Notes
s from a region or set


## DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 191-200 | Skills and Concepts to Develop (50\% Probability*) 201-210 | Skills and Concepts to Introduce (27\% Probability*) $211-220$ |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies a fraction (denominators other than $2,3,4,8,10$ ) from a region or set | - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Identifies a decimal on a number line to the tenths place <br> - Rounds decimals to the nearest whole number <br> - Graphs ordered pairs in the first quadrant <br> - Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph) <br> - Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system <br> - Determines the distance between points, following grid lines, in the first quadrant on a coordinate graph (as in city blocks) <br> - Locates the origin on a coordinate grid | - Identifies an integer from a number line <br> - Compares two integers <br> - Orders integers on a number line <br> - Defines "integers" |
| New Vocabulary: billion, composite number, decade, deposit, each, grid, hundred million, miles per hour, prime number, quintillion, standard | New Vocabulary: biggest, coordinate, coordinate point, expanded numeral, larger, miles per gallon, origin | New Vocabulary: century, coin, common factor, decimal form, greatest common factor, how long, lowest term, lowest terms, reduce, triple |
| numeral, trilion <br> New Signs and Symbols: ( ) ordered pair, ${ }^{\circ} \mathrm{F}$ degrees Fahrenheit, g gram, $>$ greater than, lb pound, < less than, min minute, mph miles per hour, \% percent, - point, R remainder | New Signs and Symbols: ft feet, in. inch, mpg miles per gallon, - negative number | New Signs and Symbols: $\$$ dollar sign, hr hour, kg kilogram, - negative sign, $\neq$ not equal to, yd yard |

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 201-210 | Skills and Concepts to Develop (50\% Probability*) 211-220 | Skills and Concepts to Introduce (27\% Probability*) 221-230 |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships | Ratios and Proportional Relationships |

- Determines unit price
- Identifies the percent represented in a 2-D region
- Converts between inches and feet
- Solves simple problems involving measurement of length
- Estimates simple conversions involving length between the customary and metric system
- Converts between cups and pints
- Converts between cups, pints, and quarts
- Computes simple conversions among units of time (hours, days)
- Computes more difficult conversions among units of time
- Applies dimensional analysis to simple real-world problems (time)
- Solves simple problems involving miles per gallon
- Solves simple problems involving miles/kilometers per hour
- Writes the missing number in a proportion using basic facts

Perform Operations

- Multiplies a fraction by a fraction without reducing to simplest form
- Multiplies a fract


## - Solves problems involving equivalent fractions

- Solves 1 -step problems involving proportions
- Calculates basic percents of a number (e.g., $10 \%, 20 \%, 25 \%, 50 \%$, 100\%)
- Converts between inches and feet
- Converts between inches, feet, and yards
- Solves simple problems involving measurement of length
- Converts between cups, pints, quarts, and gallons
- Apply dimensional analysis to simple real-world problems (capacity)
- Computes more difficult conversions among units of time
- Applies dimensional analysis to simple real-world problems (time)
- Solves simple problems involving miles per gallon
- Determines unit price
- Solves problems involving rates
- Writes a basic percent as a fraction and vice versa (e.g., $10 \%, 25 \%$, 50\%, 100\%)
- Expresses a percent as a fraction with 100 as the denominator and vice versa
- Recognizes and writes proportions
- Identifies the percent represented in a 2-D region

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) |  |
| :--- | :---: |
| 201 - 210 |  |$|$


| Skills and Concepts to Develop (50\% Probability*) |  |
| :--- | :--- |
| $211-220$ |  |$|$

- Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Uses rounding to estimate answers to difficult multiplication and division problems (whole numbers only)
- Subtracts numbers with 5 digits or more with regrouping
- Instantly recalls basic multiplication and division facts in a table
- Multiplies a 2-digit number by a 2-digit number with regrouping
- Multiplies a 3-digit number by a 2-digit number with regrouping
- Performs mental computation with multiplication
- Uses multiplication strategies to explain computation (e.g., doubles, 9patterns, decomposing, partial products)
- Multiplies a 3-digit number by a 3-digit number
- Multiplies a 4- or more digit number by multiples of 100 or 1000
- Multiplies multiple-digit numbers
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder
- Performs mental computation with division
- Divides a 4-digit number by a 1-digit number with no remainder
- Divides a 3-digit number by a 2-digit number
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves whole number word problems with division over $10 \times 10$
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves real-world multiple-step problems involving whole numbers - Demonstrates an understanding of the inverse relationship between addition and subtraction
- Adds fractions with like denominators without reducing
- Adds fractions with like denominators with reducing or converting to a mixed fraction

Skills and Concepts to Introduce (27\% Probability*)

- Uses rounding to estimate answers to real-world problems involving
multiplication and division of numbers less than 100 (whole numbers multip
only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Multiplies multiple-digit numbers
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world multiple-step problems involving whole numbers
- Demonstrates an understanding of multiple properties
- Adds fractions with like denominators with reducing or converting to a mixed fraction
- Adds fractions with unlike denominators without reducing
- Adds fractions with unlike denominators with reducing or converting to a mixed fraction
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Adds mixed fractions where converting from improper fractions is necessary
- Subtracts fractions with like denominators with reducing
- Subtracts fractions with unlike denominators without reducing
- Subtracts fractions with unlike denominators with reducing
- Subtracts mixed fractions with unlike denominators with no regrouping - Subtracts whole numbers, fractions, and mixed fractions
- Subtracts whole numbers, fractions, and mixed fractions with regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction without reducing to simplest form (complex problem)
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number
- Multiplies mixed fractions

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability ${ }^{*}$ ) <br> $201-210$ |
| :--- |
| Perform Operations |
| - Solves real-world problems involving addition and subtraction of |

- Solves real-world problems involving addition and subtraction of integers
- Solves problems involving measurement of time
- Solves simple problems involving elapsed time, with the conversion of hours
- Solves problems using tables
- Writes a terminating decimal as a fraction or mixed number
- Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater with addition and subtraction (whole numbers only)
- Uses rounding to estimate answers to addition and subtraction
problems (whole numbers only)
- Adds multiple-digit numbers, with regrouping, with sums over 1000
- Adds multiple-digit numbers with sums under 1000
- Performs mental computation with more than 4 addends
- Subtracts 3- or 4-digit numbers with regrouping
- Subtracts numbers with 5 digits or more with regrouping
- Solves real-world whole number problems involving subtraction with numbers 100 and under (analysis)
- Solves problems using the inverse relationship between addition and subtraction
- Instantly recalls basic multiplication and division facts in a table
- Multiplies a 2-digit number by a 1-digit number with regrouping
- Multiplies a 3- or 4-digit number by a 1-digit number
- Multiplies multiple 1-digit numbers
- Multiplies a 2-digit number by a 2-digit number with regrouping
- Multiplies a 3-digit number by a 2-digit number with regrouping
- Performs mental computation with multiplication
- Multiplies a 2- or 3-digit number by multiples of 10 or 100
- Multiplies a 3-digit number by a 3-digit number
- Solves word problems involving whole number multiplication with numbers greater than $10 \times 10$
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Instantly recalls division facts with dividend and divisors less than 13 - Divides a 2-digit number by a 1-digit number with no remainder - Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder Perform Operations
- Adds fractions with unlike denominators without reducing
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)
- Subtracts fractions with unlike denominators without reducing
- Subtracts mixed fractions with unlike denominators with no regrouping - Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number
- Solves 1 -step real-world problems involving fractions with multiplication and division
- Adds decimals to the hundredths place in horizontal format (not same number of digits)
- Adds decimals to the thousandths place horizontally with and without regrouping
- Adds decimals through the hundred-thousandths place
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Computes the value of multiple bills and coins (addition/subtraction only)
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only)
- Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
- Multiplies a decimal by a decimal (factors to hundredths)
- Divides decimal by a whole number
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division)
- Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes addition and subtraction on multiple-step real-world problems involving money
- Computes addition, subtraction, multiplication, and division on multiple step, real-world problems involving money
- Adds integers with like signs
- Uses models to add and subtract integers and connect the actions to algorithms
Skills and Concepts to Introduce (27\% Probability*)
221-230


## - Divides a fraction by a fraction

- Divides a mixed fraction by a fraction
- Solves 1-step real-world problems involving fractions with multiplication and division
- Solves 2- or more step real-world problems involving fractions with multiplication and division
- Solves problems involving fractions (e.g., multiple operations conversions)
- Adds decimals to the hundredths place in horizontal format (not same number of digits)
- Adds decimals through the hundred-thousandths place
- Subtracts decimals to the hundredths place (not same number of digits)
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Subtracts decimals through the hundred-thousandths place, horizontally
- Subtracts a decimal from a whole number, horizontally
- Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
- Multiplies a decimal by a decimal (factors to hundredths)
- Multiplies a decimal by 10, 100, 1000
- Multiplies a decimal by a decimal (factors to thousandths)
- Divides a decimal by 10, 100, 1000
- Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes the value of multiple bills and coins (multiplication/division)
- Calculate the sum of integers using a number line
- Adds integers with unlike signs
- Adds several positive and negative integers
- Uses models to add and subtract integers and connect the actions to algorithms
- Subtracts integers
- Solves real-world problems involving addition and subtraction of integers
- Solves problems involving addition and subtraction of integers
- Multiplies integers with unlike signs
- Divides integers with unlike signs
- Divides integers with like signs
- Adds rational expressions in decimal form
- Identifies the additive inverse property

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 201-210 | Skills and Concepts to Develop (50\% Probability*) 211-220 | Skills and Concepts to Introduce (27\% Probability*) 221-230 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
|  | - Solves real-world problems involving addition and subtraction of integers <br> - Multiplies integers with unlike signs <br> - Divides integers with unlike signs <br> - Divides integers with like signs <br> - Demonstrates an understanding that division by 0 is undefined <br> - Solves difficult problems involving elapsed time, with the conversion of hours <br> - Selects and uses the appropriate units depending on degree of accuracy required to solve problems <br> - Expresses a simple fraction as a decimal <br> - Writes a simple mixed fraction as a decimal and vice versa <br> - Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10 <br> - Expresses a percent as a decimal and vice versa <br> - Expresses the equivalent form of a fraction, decimal, and/or percent (simple fraction) <br> - Determines factors of whole numbers <br> - Identifies numbers as prime <br> - Identifies common factors of two or more numbers <br> - Identifies the greatest common factor of whole numbers | - Solves difficult problems involving elapsed time, with the conversion of hours <br> - Interprets data given in tables to solve problems <br> - Writes a simple mixed fraction as a decimal and vice versa <br> - Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10 <br> - Determines factors of whole numbers <br> - Uses multiple number theory concepts to solve problems (e.g., factors, digits, odd/even, divisibility) <br> - Uses factor and multiple concepts to solve simple problems <br> - Identifies common factors of two or more numbers <br> - Identifies the greatest common factor of whole numbers |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies the numeral and written name for whole numbers over 100,000 <br> - Compares whole numbers through the billions using the symbols <, >, or $=$ <br> - Orders whole numbers a million or greater using < or > symbols <br> - Rounds 4 -, 5 -, and 6 -digit whole numbers to the nearest ten <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand <br> - Rounds whole numbers to the nearest hundred thousand <br> - Rounds wholes numbers to the nearest billion <br> - Compares integers on a number line <br> - Explains the rules for rounding <br> - Writes equivalent forms of whole numbers using place value (e.g., $54=$ 4 tens and 14 ones) <br> - Identifies the place value and value of each digit in whole numbers through the billions <br> - Writes whole numbers in standard and expanded form through the hundred thousands | - Converts fractions to lowest terms <br> - Predicts the relative size of the answer when computing with 10 's, 100's, 1000's <br> - Predicts the relative size of the answer when multiplying whole numbers <br> - Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system <br> - Locates the origin on a coordinate grid <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest hundred <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest thousand <br> - Rounds 4-, 5-, and 6-digit whole numbers to the nearest ten thousand <br> - Rounds wholes numbers to the nearest billion <br> - Writes whole numbers in standard and expanded form through the hundred thousands <br> - Identifies equivalent fractions using visual representations <br> - Identifies a fractions in lowest terms from a region or set <br> - Identifies eighths, reduced to lowest terms, from a region or set <br> - Determines simple equivalent fractions using multiples | - Graphs ordered pairs in all quadrants <br> - Writes equivalent forms of whole numbers using place value (numbers 100 or greater) (e.g., $253=2$ hundreds, 5 tens, and 3 ones) <br> - Writes whole numbers in standard and exponential form <br> - Identifies a fractions in lowest terms from a region or set <br> - Rounds decimals to nearest thousandth <br> - Determines simple equivalent fractions using multiples <br> - Determines equivalent fractions using multiples <br> - Compares fractions (e.g., comparing numerators and denominators) <br> - Uses alternative algorithms to explain the meaning of "fraction" <br> - Represents a decimal to thousandths place (e.g., three thousandths = 0.003) <br> - Represents a decimal to the hundred thousandths place - (e.g., three hundred thousandths $=0.00003$ ) <br> - Writes a decimal for a shaded region to the hundredths place <br> - Compares and orders decimals to the hundredths place (not same number of digits after decimal) |

Explanatory Notes


DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 201-210 | Skills and Concepts to Develop (50\% Probability*) 211-220 | Skills and Concepts to Introduce (27\% Probability*) 221-230 |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Applies base ten place value concepts with whole numbers to solve problems <br> - Writes whole numbers using place value terms and vice versa <br> - Identifies halves of a region using nonadjacent parts <br> - Identifies equivalent fractions using visual representations <br> - Expresses "1" in many different ways (e.g., 3/3, 4/4) <br> - Converts a basic fractional numeral to lowest terms (e.g., halves, thirds, quarters) <br> - Writes mixed numbers as improper fractions and improper fractions as mixed numbers <br> - Compares fractions (e.g., common denominator, 1 in the numerator, denominator is $2,3,4,6,8,10$ ) <br> - Identifies whole numbers over 999 using base-10 blocks <br> - Identifies the numeral and written name for whole numbers with a zero between digits to the ten thousands place <br> - Orders fractions on a number line <br> - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Identifies a decimal on a number line to the tenths place <br> - Rounds decimals to the nearest whole number <br> - Graphs ordered pairs in the first quadrant <br> - Determines and names locations in the first quadrant on a labeled grid or coordinate system (e.g., map or graph) <br> - Determines the distance between horizontal and vertical lines in the first quadrant of a rectangular coordinate system <br> - Determines the distance between points, following grid lines, in the first quadrant on a coordinate graph (as in city blocks) <br> - Locates the origin on a coordinate grid | - Writes mixed numbers as improper fractions and improper fractions as mixed numbers <br> - Compares fractions on a number line <br> - Compares fractions greater than or less than a given fraction using visual representations <br> - Compares fractions and mixed numbers <br> - Compares fractions and mixed numbers using symbols <br> - Orders fractions on a number line <br> - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Represents a decimal to the hundredths place (e.g., three hundredths = 0.03) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest whole number <br> - Rounds decimals to the nearest tenth <br> - Applies base ten place value concepts to solve problems using decimals <br> - Identifies an integer from a number line <br> - Compares two integers <br> - Orders integers on a number line <br> - Defines "integers" | - Compares and orders decimals to the thousandths place (not same number of digits after decimal) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest hundredth <br> - Identifies the place value and value of each digit to the hundredths and thousandths <br> - Applies base ten place value concepts to solve problems using decimals <br> - Compares two integers <br> - Orders integers on a number line <br> - Orders integers <br> - Locates rational numbers on a number line <br> - Orders rational numbers, in $a / b$ form <br> - Orders fractions and decimals to the hundred thousandths <br> - Determines the relative magnitude of whole numbers <br> - Rounds whole numbers to the nearest million <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) |
| New Vocabulary: biggest, coordinate, coordinate point, expanded numeral, larger, miles per gallon, origin | New Vocabulary: century, coin, common factor, decimal form, greatest common factor, how long, lowest term, lowest terms, reduce, triple | New Vocabulary: real number, ten million |
| New Signs and Symbols: ft feet, in. inch, mpg miles per gallon, - negative number | New Signs and Symbols: \$ dollar sign, hr hour, kg kilogram, - negative sign, $\neq$ not equal to, yd yard | centimeter/centimetre, ${ }^{\circ} \mathrm{C}$ degrees Celsius, km kilometer/kilometre, mL milliliter/millilitre, \# number, / per, + positive number, : ratio |

## Explanatory Notes


appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 211-220 | Skills and Concepts to Develop (50\% Probability*) 221-230 | Skills and Concepts to Introduce (27\% Probability*) 231-240 |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships | Ratios and Proportional Relationships |

- Solves problems involving equivalent fractions
- Solves 1 -step problems involving proportions
- Calculates basic percents of a number (e.g., 10\%, 20\%, 25\%, 50\%, 100\%)
- Converts between inches and feet
- Converts between inches, feet, and yards
- Solves simple problems involving measurement of length
- Converts between cups, pints, quarts, and gallons
- Apply dimensional analysis to simple real-world problems (capacity)
- Computes more difficult conversions among units of time
- Applies dimensional analysis to simple real-world problems (time)
- Solves simple problems involving miles per gallon
- Determines unit price
- Solves problems involving rates
- Writes a basic percent as a fraction and vice versa (e.g., 10\%, 25\%, 50\%, 100\%)
- Expresses a percent as a fraction with 100 as the denominator and vice versa
- Recognizes and writes proportions
- Identifies the percent represented in a 2-D region
- Solves real-world problems involving decimals (not money) using multiplication
- Solves problems involving ratios
- Solves 1 -step problems involving proportions
- Calculates basic percents of a number (e.g., $10 \%, 20 \%, 25 \%, 50 \%$,

100\%)

- Calculates a percent of a number (e.g., $6 \%$ of 30 )
- Calculates a number from a percent (e.g., 4 is $9 \%$ of what)
- Solves problems involving percents
- Solves problems involving tax and tips
- Converts between inches, feet, and yards
- Converts between millimeters, centimeters, meters, and kilometers
- Uses dimensional analysis for unit conversions (length)
- Uses concrete and pictorial models to represent ratios
- Solves problems involving length in the customary system and
converts to larger or smaller units
- Converts between ounces and pounds
- Converts between ounces, pounds, and tons
- Converts between cups, pints, quarts, and gallons
- Converts within the metric system
- Apply dimensional analysis to simple real-world problems (capacity)
- Solves problems involving capacity in the customary system and converts to larger or smaller units
- Computes 2-step conversions between units of time
- Applies dimensional analysis to simple real-world problems (time)
- Writes the missing number in a proportion with numbers other than basic facts (e.g., 5/13=?/117)
- Solves complex problems involving miles per gallon
- Solves complex problems involving miles/kilometers per hour
- Solves problems involving rates
- Solves problems involving perimeter and converts to larger or smaller units
- Expresses a percent as a fraction and vice versa
- Interprets data given in circle graphs to solve complex problems (with percents)
- Writes a ratio as a percent and vice versa
- Writes a ratio as a percent and vice versa
- Identifies the ratio from a given real-world situation
- Uses estimation to solve problems involving proportional reasoning (decimals only)
- Solves real-world problems involving decimals (not money) using multiplication
- Solves problems involving equivalent fractions (analysis)
- Solves problems involving ratios
- Solves multiple-step problems involving proportions
- Calculates a percent of a number (e.g., $6 \%$ of 30 )
- Calculates the percent one number is of another (e.g., 20 is what \% of 90)
- Solves problems involving percents
- Solves problems involving percents (analysis)
- Solves problems involving simple percent discounts (e.g., finding sale price)
- Solves problems involving percent increase and decrease
- Solves problems involving tax and tips
- Calculates commission/deductions and total pay
- Converts between millimeters, centimeters, meters, and kilometers
- Uses dimensional analysis for unit conversions (length)
- Converts between the customary and metric system given conversion ratios (2-step, length)
- Apply dimensional analysis to simple real-world problems (length)
- Solves problems involving length in the customary system and converts to larger or smaller units
- Converts between grams and kilograms
- Solves problems involving weight in the customary system and converts to larger or smaller units
- Converts within the metric system
- Apply dimensional analysis to simple real-world problems (capacity)
- Solves problems involving capacity in the customary system and converts to larger or smaller units
- Solves complex problems involving miles per gallon
- Solves problems comparing unit prices
- Solves problems involving rates
- Interprets data given in circle graphs to solve complex problems (with percents)
- Expresses a percent as a fraction and vice versa

| Skills and concepts to Enhance (73\% Probability*) |  |
| :--- | :---: |
| $211-\mathbf{2 2 0}$ |  |

- Subtracts mixed fractions with like denominators with no regrouping - Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Uses rounding to estimate answers to difficult multiplication and division problems (whole numbers only)
- Subtracts numbers with 5 digits or more with regrouping
- Instantly recalls basic multiplication and division facts in a table
- Multiplies a 2-digit number by a 2-digit number with regrouping
- Multiplies a 3-digit number by a 2-digit number with regrouping
- Performs mental computation with multiplication
- Uses multiplication strategies to explain computation (e.g., doubles, 9patterns, decomposing, partial products)
- Multiplies a 3-digit number by a 3-digit number
- Multiplies a 4- or more digit number by multiples of 100 or 1000
- Multiplies multiple-digit numbers
- Models whole number multiplication and division algorithms (e.g., uses physical materials to show 4 groups of 3 objects)
- Divides a 2-digit number or a 3-digit number by a 1-digit number with a remainder
- Performs mental computation with division
- Divides a 4-digit number by a 1 -digit number with no remainder
- Divides a 3-digit number by a 2-digit number
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves whole number word problems with division over $10 \times 10$ - Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world problems involving 2-step multiple operations, whole numbers only
- Solves real-world multiple-step problems involving whole numbers
- Demonstrates an understanding of the inverse relationship between addition and subtraction
- Adds fractions with like denominators without reducing
$\left.\begin{array}{|l|l}\text { Skills and Concepts to Develop (50\% Probability*) } \\ \text { 221-230 }\end{array}\right)$
- Divides a decimal by a decimal
- Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only)
- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Multiplies multiple-digit numbers
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world multiple-step problems involving whole numbers
- Demonstrates an understanding of multiple properties
- Adds fractions with like denominators with reducing or converting to a mixed fraction
- Adds fractions with unlike denominators without reducing
- Adds fractions with unlike denominators with reducing or converting to a mixed fraction
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Adds mixed fractions where converting from improper fractions is necessary
- Subtracts fractions with like denominators with reducing
- Subtracts fractions with unlike denominators without reducing
- Subtracts fractions with unlike denominators with reducing
- Subtracts mixed fractions with unlike denominators with no regrouping
- Subtracts whole numbers, fractions, and mixed fractions
- Subtracts whole numbers, fractions, and mixed fractions with regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction without reducing to simplest form (complex problem)
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number


## - Identifies the additive inverse property

- Divides multiple-digit numbers
- Divides numbers by powers of 10
- Adds fractions with unlike denominators with reducing or converting to a mixed fraction
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Adds mixed fractions where converting from improper fractions is necessary
- Subtracts whole numbers, fractions, and mixed fractions
- Subtracts whole numbers, fractions, and mixed fractions with regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting both denominators is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies mixed fractions
- Uses models to multiply and divide fractions and mixed fractions and connect the actions to algorithms
- Divides a fraction by a fraction
- Divides a fraction by a whole number
- Divides a whole number by a fraction
- Divides a mixed fraction by a whole numbe
- Divides a whole number by a mixed fraction
- Divides a mixed fraction by a fraction
- Divides a fraction by a mixed fraction
- Divides a mixed fraction by a mixed fraction
- Solves 2- or more step real-world problems involving fractions with multiplication and division
- Solves problems involving fractions (e.g., multiple operations conversions)
- Subtracts a decimal from a whole number, horizontally
- Multiplies a decimal by 10, 100, 1000
- Divides a whole number by a decimal
- Divides a decimal by 10, 100, 1000
- Divides a decimal by a decimal
- Adds integers with unlike signs
- Adds several positive and negative integers
- Subtracts integers
- Solves problems involving addition and subtraction of integers

Goal: The Real and Complex Number Systems
Skills and concepts to Enhance (73\% Probability*)
211-220

- Adds fractions with like denominators with reducing or converting to a mixed fraction
- Adds fractions with unlike denominators without reducing
- Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths)
- Subtracts simple fractions with unlike denominators without reducing (e.g., halves, quarters, thirds, eighths)
- Subtracts fractions with unlike denominators without reducing
- Subtracts mixed fractions with unlike denominators with no regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number
- Solves 1-step real-world problems involving fractions with multiplication and division
- Adds decimals to the hundredths place in horizontal format (not same number of digits)
- Adds decimals to the thousandths place horizontally with and without regrouping
- Adds decimals through the hundred-thousandths place
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Computes the value of multiple bills and coins (addition/subtraction only)
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (addition/subtraction only)
- Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
- Multiplies a decimal by a decimal (factors to hundredths)
- Divides decimal by a whole number
- Analyzes and computes 1 operation on real-world problems involving money over $\$ 5.00$ (multiplication/division)
- Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes addition and subtraction on multiple-step real-world problems involving money
- Computes addition, subtraction, multiplication, and division on multiplestep, real-world problems involving money
- Adds integers with like signs
Perform Operations


## - Multiplies mixed fractions

## - Divides a fraction by a fraction

- Divides a mixed fraction by a fraction
- Solves 1 -step real-world problems involving fractions with multiplication and division
- Solves 2- or more step real-world problems involving fractions with multiplication and division
- Solves problems involving fractions (e.g., multiple operations conversions)
- Adds decimals to the hundredths place in horizontal format (not same number of digits)
- Adds decimals through the hundred-thousandths place
- Subtracts decimals to the hundredths place (not same number of digits)
- Subtracts decimals to the thousandths place, horizontally, with and without regrouping
- Subtracts decimals through the hundred-thousandths place, horizontally
- Subtracts a decimal from a whole number, horizontally
- Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths)
- Multiplies a decimal by a decimal (factors to hundredths)
- Multiplies a decimal by 10, 100, 1000
- Multiplies a decimal by a decimal (factors to thousandths)
- Divides a decimal by 10, 100, 1000
- Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division)
- Computes the value of multiple bills and coins (multiplication/division)
- Calculate the sum of integers using a number line
- Adds integers with unlike signs
- Adds several positive and negative integers
- Uses models to add and subtract integers and connect the actions to algorithms
- Subtracts integers
- Solves real-world problems involving addition and subtraction of integers
- Solves problems involving addition and subtraction of integers
- Multiplies integers with unlike signs
- Divides integers with unlike signs
- Divides integers with like signs
- Adds rational expressions in decimal form

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

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## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $211-220$ | Skills and Concepts to Develop (50\% Probability*) 221-230 | Skills and Concepts to Introduce (27\% Probability*) $231-240$ |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Identifies eighths, reduced to lowest terms, from a region or set <br> - Determines simple equivalent fractions using multiples <br> - Writes mixed numbers as improper fractions and improper fractions as mixed numbers <br> - Compares fractions on a number line <br> - Compares fractions greater than or less than a given fraction using visual representations <br> - Compares fractions and mixed numbers <br> - Compares fractions and mixed numbers using symbols <br> - Orders fractions on a number line <br> - Explains different interpretations of fractions (e.g., parts of a whole, parts of a set, and division of whole numbers by whole numbers) <br> - Represents a decimal to the hundredths place (e.g., three hundredths = 0.03) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest whole number <br> - Rounds decimals to the nearest tenth <br> - Applies base ten place value concepts to solve problems using decimals <br> - Identifies an integer from a number line <br> - Compares two integers <br> - Orders integers on a number line <br> - Defines "integers" | - Compares and orders decimals to the hundredths place (not same number of digits after decimal) <br> - Compares and orders decimals to the thousandths place (not same number of digits after decimal) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest hundredth <br> - Identifies the place value and value of each digit to the hundredths and thousandths <br> - Applies base ten place value concepts to solve problems using decimals <br> - Compares two integers <br> - Orders integers on a number line <br> - Orders integers <br> - Locates rational numbers on a number line <br> - Orders rational numbers, in $a / b$ form <br> - Orders fractions and decimals to the hundred thousandths <br> - Determines the relative magnitude of whole numbers <br> - Rounds whole numbers to the nearest million <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) |  |
| New Vocabulary: century, coin, common factor, decimal form, greatest common factor, how long, lowest term, lowest terms, reduce, triple | New Vocabulary: real number, ten million | New Vocabulary: discount, equality |
| common factor, how long, lowest term, lowest terms, reduce, triple New Signs and Symbols: \$ dollar sign, hr hour, kg kilogram, - negative sign, $\neq$ not equal to, yd yard | New Signs and Symbols: ( ) parenthesis around an integer, cm centimeter/centimetre, ${ }^{\circ} \mathrm{C}$ degrees Celsius, km kilometer/kilometre, mL milliliter/millilitre, \# number, / per, + positive number, : ratio | New Signs and Symbols: \|| absolute value, oz ounce |

Skills and concepts to Enhance (73\% Probability*)
$221-230$

- Solves real-world problems involving decimals (not money) using multiplication
- Solves problems involving ratios
- Solves 1-step problems involving proportions
- Calculates basic percents of a number (e.g., $10 \%, 20 \%, 25 \%, 50 \%$, 100\%)
- Calculates a percent of a number (e.g., $6 \%$ of 30 )
- Calculates a number from a percent (e.g., 4 is $9 \%$ of what)
- Solves problems involving percents
- Solves problems involving tax and tips
- Converts between inches, feet, and yards
- Converts between millimeters, centimeters, meters, and kilometers
- Uses dimensional analysis for unit conversions (length)
- Uses concrete and pictorial models to represent ratios
- Solves problems involving length in the customary system and converts to larger or smaller units
- Converts between ounces and pounds
- Converts between ounces, pounds, and tons
- Converts between cups, pints, quarts, and gallons
- Converts within the metric system
- Apply dimensional analysis to simple real-world problems (capacity)
- Solves problems involving capacity in the customary system and converts to larger or smaller units
- Computes 2-step conversions between units of time
- Applies dimensional analysis to simple real-world problems (time)
- Writes the missing number in a proportion with numbers other than basic facts (e.g., 5/13=?/117)
- Solves complex problems involving miles per gallon
- Solves complex problems involving miles/kilometers per hour
- Solves problems involving rates
- Solves problems involving perimeter and converts to larger or smaller units
- Expresses a percent as a fraction and vice versa
- Interprets data given in circle graphs to solve complex problems (with percents)
- Writes a ratio as a percent and vice versa

Skills and Concepts to Develop (50\% Probability*)

- Writes a ratio as a percent and vice versa
- Identifies the ratio from a given real-world situation
- Uses estimation to solve problems involving proportional reasoning (decimals only)
- Solves real-world problems involving decimals (not money) using multiplication
- Solves problems involving equivalent fractions (analysis)
- Solves problems involving ratios
- Solves multiple-step problems involving proportions
- Calculates a percent of a number (e.g., $6 \%$ of 30 )
- Calculates the percent one number is of another (e.g., 20 is what \% of 90)
- Solves problems involving percents
- Solves problems involving percents (analysis)
- Solves problems involving simple percent discounts (e.g., finding sale price)
- Solves problems involving percent increase and decrease
- Solves problems involving tax and tips
- Calculates commission/deductions and total pay
- Converts between millimeters, centimeters, meters, and kilometers
- Uses dimensional analysis for unit conversions (length)
- Converts between the customary and metric system given conversion ratios (2-step, length)
- Apply dimensional analysis to simple real-world problems (length)
- Solves problems involving length in the customary system and converts to larger or smaller units
- Converts between grams and kilograms
- Solves problems involving weight in the customary system and converts to larger or smaller units
- Converts within the metric system
- Apply dimensional analysis to simple real-world problems (capacity)
- Solves problems involving capacity in the customary system and converts to larger or smaller units
- Solves complex problems involving miles per gallon
- Solves problems comparing unit prices
- Solves problems involving rates
- Interprets data given in circle graphs to solve complex problems (with percents)
- Expresses a percent as a fraction and vice versa
- Solves real-world problems involving decimals (not money) using multiplication
- Solves multiple-step problems involving proportions
- Solves problems involving a fractional increase
- Calculates the percent one number is of another (e.g., 20 is what \% of 90)
- Calculates a percent of a rational number (e.g., $6 \%$ of 0.78 )
- Solves problems involving percents (analysis)
- Solves problems involving simple percent discounts (e.g., finding sale price)
- Solves problems involving complex percent discounts (e.g., finding percent discount, regular price)
- Calculates commission/deductions and total pay
- Solves problems involving successive discounts
- Uses dimensional analysis for unit conversions (length)
- Apply dimensional analysis to simple real-world problems (length) - Solves problems involving weight in the customary system and converts to larger or smaller units
- Uses dimensional analysis for unit conversions (time)
- Solves problems involving rate conversions (e.g., mi/hr to ft/sec)
- Identifies the ratio from a given real-world situation

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 221-230 | Skills and Concepts to Develop (50\% Probability*) 231-240 | Skills and Concepts to Introduce (27\% Probability*) 241-250 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
| - Divides a decimal by a decimal <br> - Uses rounding to estimate answers to real-world problems involving multiplication and division of numbers less than 100 (whole numbers only) <br> - Uses rounding to estimate answers to real-world problems involving numbers less than 1000 with multiplication and division (whole numbers only) | - Identifies the additive inverse property <br> - Divides multiple-digit numbers <br> - Divides numbers by powers of 10 <br> - Adds fractions with unlike denominators with reducing or converting to a mixed fraction <br> - Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths) | - Subtracts integers <br> - Uses a number line to determine the distance between a positive and negative number <br> - Uses the multiplicative inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Identifies the least common multiple of whole numbers |

- Uses rounding to estimate answers to real-world problems involving numbers 1000 or greater using multiplication and division (whole numbers only)
- Multiplies multiple-digit numbers
- Divides a 4-digit number by a 2-digit number
- Divides multiple-digit numbers
- Solves complex word problems involving whole number division with remainder (e.g., 2-step, 2-digit divisor)
- Solves real-world multiple-step problems involving whole numbers
- Demonstrates an understanding of multiple properties
- Adds fractions with like denominators with reducing or converting to a mixed fraction
- Adds fractions with unlike denominators without reducing
- Adds fractions with unlike denominators with reducing or converting to a mixed fraction
- Adds simple mixed fractions with unlike denominators (e.g., halves thirds, fourths, eighths)
- Adds mixed fractions where converting from improper fractions is necessary
- Subtracts fractions with like denominators with reducing
- Subtracts fractions with unlike denominators without reducing
- Subtracts fractions with unlike denominators with reducing
- Subtracts mixed fractions with unlike denominators with no regrouping
- Subtracts whole numbers, fractions, and mixed fractions
- Subtracts whole numbers, fractions, and mixed fractions with regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting one denominator is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies a fraction by a fraction without reducing to simplest form (complex problem)
- Multiplies a fraction by a fraction where reducing to simplest form is necessary
- Multiplies a fraction by a whole number


DesCartes: A Continuum of Learning ${ }^{\circledR}$
Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $221-230$ | Skills and Concepts to Develop (50\% Probability*) 231-240 | Skills and Concepts to Introduce (27\% Probability*) 241-250 |
| :---: | :---: | :---: |
| Perform Operation | Perform Operations | Perform Operations |
| - Multiplies mixed fractions <br> - Divides a fraction by a fraction <br> - Divides a mixed fraction by a fraction <br> - Solves 1-step real-world problems involving fractions with multiplication and division <br> - Solves 2- or more step real-world problems involving fractions with multiplication and division <br> - Solves problems involving fractions (e.g., multiple operations, conversions) <br> - Adds decimals to the hundredths place in horizontal format (not same number of digits) <br> - Adds decimals through the hundred-thousandths place <br> - Subtracts decimals to the hundredths place (not same number of digits) <br> - Subtracts decimals to the thousandths place, horizontally, with and without regrouping <br> - Subtracts decimals through the hundred-thousandths place, horizontally <br> - Subtracts a decimal from a whole number, horizontally <br> - Multiplies a decimal by a decimal, vertical form (factors to tenths or hundredths) <br> - Multiplies a decimal by a decimal (factors to hundredths) <br> - Multiplies a decimal by 10, 100, 1000 <br> - Multiplies a decimal by a decimal (factors to thousandths) <br> - Divides a decimal by 10, 100, 1000 <br> - Computes with dollars and cents over $\$ 5.00$ and converts to decimals (multiplication/division) <br> - Computes the value of multiple bills and coins (multiplication/division) <br> - Calculate the sum of integers using a number line <br> - Adds integers with unlike signs <br> - Adds several positive and negative integers <br> - Uses models to add and subtract integers and connect the actions to algorithms <br> - Subtracts integers <br> - Solves real-world problems involving addition and subtraction of integers <br> - Solves problems involving addition and subtraction of integers <br> - Multiplies integers with unlike signs <br> - Divides integers with unlike signs <br> - Divides integers with like signs <br> - Adds rational expressions in decimal form | - Multiplies integers with like signs <br> - Divides integers with like signs <br> - Subtracts rational expressions in decimal form <br> - Multiplies rational expressions <br> - Interprets data given in tables to solve problems <br> - Writes a fraction as a decimal and vice versa <br> - Writes a fraction as a mixed decimal and vice versa |  |

## Explanatory Notes

 appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version

DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 221-230 | Skills and Concepts to Develop (50\% Probability*) $231-240$ | Skills and Concepts to Introduce (27\% Probability*) 241-250 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
| - Identifies the additive inverse property <br> - Solves difficult problems involving elapsed time, with the conversion of hours <br> - Interprets data given in tables to solve problems <br> - Writes a simple mixed fraction as a decimal and vice versa <br> -Writes a fraction or mixed number as a decimal when the denominator is a multiple of 10 <br> - Determines factors of whole numbers <br> - Uses multiple number theory concepts to solve problems (e.g., factors, digits, odd/even, divisibility) <br> - Uses factor and multiple concepts to solve simple problems <br> - Identifies common factors of two or more numbers <br> - Identifies the greatest common factor of whole numbers |  |  |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Graphs ordered pairs in all quadrants <br> - Writes equivalent forms of whole numbers using place value (numbers 100 or greater) (e.g., $253=2$ hundreds, 5 tens, and 3 ones) <br> - Writes whole numbers in standard and exponential form <br> - Identifies a fractions in lowest terms from a region or set <br> - Rounds decimals to nearest thousandth <br> - Determines simple equivalent fractions using multiples <br> - Determines equivalent fractions using multiples <br> - Compares fractions (e.g., comparing numerators and denominators) <br> - Uses alternative algorithms to explain the meaning of "fraction" <br> - Represents a decimal to thousandths place (e.g., three thousandths = 0.003) <br> - Represents a decimal to the hundred thousandths place - (e.g., three hundred thousandths $=0.00003$ ) <br> - Writes a decimal for a shaded region to the hundredths place <br> - Compares and orders decimals to the hundredths place (not same number of digits after decimal) <br> - Compares and orders decimals to the thousandths place (not same number of digits after decimal) <br> - Compares and orders decimals past the thousandths place <br> - Rounds decimals to the nearest hundredth <br> - Identifies the place value and value of each digit to the hundredths and thousandths <br> - Applies base ten place value concepts to solve problems using decimals <br> - Compares two integers | - Graphs ordered pairs in all quadrants <br> - Simplifies rational expressions with absolute value <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) <br> - Determines the relative magnitude of whole numbers <br> - Writes whole numbers in standard and exponential form <br> - Compares fractions (e.g., comparing numerators and denominators) <br> - Rounds decimals to the nearest hundredth <br> - Compares and orders decimal and fractional coordinates on a number line | - Simplifies expressions containing square roots <br> - Estimates the square roots of numbers <br> - Uses expressions with absolute value to represent situations <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) |

## Explanatory Notes


appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.

## DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 221-230 | Skills and Concepts to Develop (50\% Probability*) $231-240$ | Skills and Concepts to Introduce (27\% Probability*) 241-250 |
| :---: | :---: | :---: |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Orders integers on a number line <br> - Orders integers <br> - Locates rational numbers on a number line <br> - Orders rational numbers, in a/b form <br> - Orders fractions and decimals to the hundred thousandths <br> - Determines the relative magnitude of whole numbers <br> - Rounds whole numbers to the nearest million <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) |  |  |
| New Vocabulary: real number, ten million | New Vocabulary: discount, equality | New Vocabulary: feet per second, least common multiple |
| New Signs and Symbols: ( ) parenthesis around an integer, cm centimeter/centimetre, ${ }^{\circ} \mathrm{C}$ degrees Celsius, km kilometer/kilometre, mL milliliter/millilitre, \# number, / per, + positive number, : ratio | New Signs and Symbols: \|| absolute value, oz ounce | New Signs and Symbols: LCM lowest common multiple, sec second, square root symbol |

## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 231-240 | Skills and Concepts to Develop (50\% Probability*) 241-250 | Skills and Concepts to Introduce (27\% Probability*) 251-260 |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships | Ratios and Proportional Relationships |
| - Writes a ratio as a percent and vice versa <br> - Identifies the ratio from a given real-world situation <br> - Uses estimation to solve problems involving proportional reasoning (decimals only) <br> - Solves real-world problems involving decimals (not money) using multiplication | - Solves real-world problems involving decimals (not money) using multiplication <br> - Solves multiple-step problems involving proportions <br> - Solves problems involving a fractional increase <br> - Calculates the percent one number is of another (e.g., 20 is what \% of 90) | - Solves problems involving successive discounts <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) <br> - Solves problems involving complex percent discounts (e.g., finding percent discount, regular price) <br> - Uses dimensional analysis for unit conversions (time) |

- Solves problems involving equivalent fractions (analysis)
- Solves problems involving ratios
- Solves multiple-step problems involving proportions
- Calculates a percent of a number (e.g., $6 \%$ of 30 )
- Calculates the percent one number is of another (e.g., 20 is what \% of 90)
- Solves problems involving percents
- Solves problems involving percents (analysis)
- Solves problems involving simple percent discounts (e.g., finding sale price)
- Solves problems involving percent increase and decrease
- Solves problems involving tax and tips
- Calculates commission/deductions and total pay
- Converts between millimeters, centimeters, meters, and kilometers
- Uses dimensional analysis for unit conversions (length)
- Converts between the customary and metric system given conversion ratios (2-step, length)
- Apply dimensional analysis to simple real-world problems (length)
- Solves problems involving length in the customary system and converts to larger or smaller units
- Converts between grams and kilograms
- Solves problems involving weight in the customary system and converts to larger or smaller units
- Converts within the metric system
- Apply dimensional analysis to simple real-world problems (capacity)
- Solves problems involving capacity in the customary system and converts to larger or smaller units
- Solves complex problems involving miles per gallon
- Solves problems comparing unit prices
- Solves problems involving rates
- Interprets data given in circle graphs to solve complex problems (with percents)
- Expresses a percent as a fraction and vice versa
- Calculates a percent of a rational number (e.g., $6 \%$ of 0.78 )
- Solves problems involving percents (analysis)
- Solves problems involving simple percent discounts (e.g., finding sale price)
- Solves problems involving complex percent discounts (e.g., finding percent discount, regular price)
- Calculates commission/deductions and total pay
- Solves problems involving successive discounts
- Uses dimensional analysis for unit conversions (length)
- Apply dimensional analysis to simple real-world problems (length)
- Solves problems involving weight in the customary system and converts to larger or smaller units
- Uses dimensional analysis for unit conversions (time)
- Solves problems involving rate conversions (e.g., mi/hr to ft/sec)
- Identifies the ratio from a given real-world situation
- Uses dimensional analysis for unit conversions (time)


## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) $231-240$ | Skills and Concepts to Develop (50\% Probability*) $241-250$ | Skills and Concepts to Introduce (27\% Probability*) $251-260$ |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
| - Identifies the additive inverse property <br> - Divides multiple-digit numbers <br> - Divides numbers by powers of 10 <br> - Adds fractions with unlike denominators with reducing or converting to a mixed fraction <br> - Adds simple mixed fractions with unlike denominators (e.g., halves, thirds, fourths, eighths) <br> - Adds mixed fractions where converting from improper fractions is necessary <br> - Subtracts whole numbers, fractions, and mixed fractions <br> - Subtracts whole numbers, fractions, and mixed fractions with regrouping <br> - Solves real-world problems involving addition and subtraction of fractions where converting both denominators is necessary <br> - Uses models to multiply and divide fractions and connect the actions to algorithms <br> - Multiplies mixed fractions <br> - Uses models to multiply and divide fractions and mixed fractions and connect the actions to algorithms <br> - Divides a fraction by a fraction <br> - Divides a fraction by a whole number <br> - Divides a whole number by a fraction <br> - Divides a mixed fraction by a whole number <br> - Divides a whole number by a mixed fraction <br> - Divides a mixed fraction by a fraction <br> - Divides a fraction by a mixed fraction <br> - Divides a mixed fraction by a mixed fraction <br> - Solves 2 - or more step real-world problems involving fractions with multiplication and division <br> - Solves problems involving fractions (e.g., multiple operations, conversions) <br> - Subtracts a decimal from a whole number, horizontally <br> - Multiplies a decimal by 10, 100, 1000 <br> - Divides a whole number by a decimal <br> - Divides a decimal by 10, 100, 1000 <br> - Divides a decimal by a decimal <br> - Adds integers with unlike signs <br> - Adds several positive and negative integers <br> - Subtracts integers <br> - Solves problems involving addition and subtraction of integers | - Subtracts integers <br> - Uses a number line to determine the distance between a positive and negative number <br> - Uses the multiplicative inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Identifies the least common multiple of whole numbers | - Uses the additive inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Performs operations on complex numbers and expresses the results in simplest form |

- Adds simple mixed fractions with unlike denominators (e.g., halves

Uses factor and mutiple concept to solve dificut problems
Identifies the least common multiple of whole numbers thirds, fourths, eighths)

- Adds mixed fractions where converting from improper fractions is necessary
- Subtracts whole numbers, fractions, and mixed fractions
- Subtracts whole numbers, fractions, and mixed fractions with regrouping
- Solves real-world problems involving addition and subtraction of fractions where converting both denominators is necessary
- Uses models to multiply and divide fractions and connect the actions to algorithms
- Multiplies mixed fractions
- Uses models to multiply and divide fractions and mixed fractions and connect the actions to algorithms
- Divides a fraction by a fraction
- Divides a fraction by a whole number
- Divides a whole number by a fraction
- Divides a mixed fraction by a whole number
- Divides a whole number by a mixed fraction
- Divides a mixed fraction by a fraction
- Divides a fraction by a mixed fraction
- Divides a mixed fraction by a mixed fraction
- Solves 2 - or more step real-world problems involving fractions with multiplication and division
- Solves problems involving fractions (e.g., multiple operations, conversions)
- Subtracts a decimal from a whole number, horizontally
- Multiplies a decimal by 10, 100, 1000
- Divides a whole number by a decimal
- Divides a decimal by 10, 100, 1000
- Divides a decimal by a decimal
- Adds integers with unlike signs
- Adds several positive and negative integers
- Subtracts integers
- Solves problems involving addition and subtraction of integers


## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 231-240 | Skills and Concepts to Develop (50\% Probability*) 241-250 | Skills and Concepts to Introduce (27\% Probability*) 251-260 |
| :---: | :---: | :---: |
| Perform Operations | Perform Operations | Perform Operations |
| - Multiplies integers with like signs <br> - Divides integers with like signs <br> - Subtracts rational expressions in decimal form <br> - Multiplies rational expressions <br> - Interprets data given in tables to solve problems <br> - Writes a fraction as a decimal and vice versa <br> - Writes a fraction as a mixed decimal and vice versa |  |  |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Graphs ordered pairs in all quadrants <br> - Simplifies rational expressions with absolute value <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) <br> - Determines the relative magnitude of whole numbers <br> - Writes whole numbers in standard and exponential form <br> - Compares fractions (e.g., comparing numerators and denominators) <br> - Rounds decimals to the nearest hundredth <br> - Compares and orders decimal and fractional coordinates on a number line | - Simplifies expressions containing square roots <br> - Estimates the square roots of numbers <br> - Uses expressions with absolute value to represent situations <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) | - Simplifies expressions containing square roots <br> - Uses expressions with absolute value to represent situations <br> - Simplifies radical expressions |
| New Vocabulary: discount, equality | New Vocabulary: feet per second, least common multiple | New Vocabulary: None |
| New Signs and Symbols: \|| absolute value, oz ounce | New Signs and Symbols: LCM lowest common multiple, sec second, square root symbol | New Signs and Symbols: i square root of -1 |

## DesCartes: A Continuum of Learning ${ }^{\circledR}$

Mathematics
Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 241-250 | Skills and Concepts to Develop (50\% Probability*) 251-260 | Skills and Concepts to Introduce (27\% Probability*) $>260$ |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships | Ratios and Proportional Relationships |
| - Solves real-world problems involving decimals (not money) using multiplication <br> - Solves multiple-step problems involving proportions <br> - Solves problems involving a fractional increase <br> - Calculates the percent one number is of another (e.g., 20 is what \% of 90) <br> - Calculates a percent of a rational number (e.g., $6 \%$ of 0.78 ) <br> - Solves problems involving percents (analysis) <br> - Solves problems involving simple percent discounts (e.g., finding sale price) <br> - Solves problems involving complex percent discounts (e.g., finding percent discount, regular price) <br> - Calculates commission/deductions and total pay <br> - Solves problems involving successive discounts <br> - Uses dimensional analysis for unit conversions (length) <br> - Apply dimensional analysis to simple real-world problems (length) <br> - Solves problems involving weight in the customary system and converts to larger or smaller units <br> - Uses dimensional analysis for unit conversions (time) <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) <br> - Identifies the ratio from a given real-world situation | - Solves problems involving successive discounts <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) <br> - Solves problems involving complex percent discounts (e.g., finding percent discount, regular price) <br> - Uses dimensional analysis for unit conversions (time) | - Solves problems involving successive discounts <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) |
| Perform Operations | Perform Operations | Perform Operations |
| - Subtracts integers <br> - Uses a number line to determine the distance between a positive and negative number <br> - Uses the multiplicative inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Identifies the least common multiple of whole numbers | - Uses the additive inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Performs operations on complex numbers and expresses the results in simplest form | - Performs operations on complex numbers and expresses the results in simplest form |
| Extend and Use Properties | Extend and Use Properties | Extend and Use Properties |
| - Simplifies expressions containing square roots <br> - Estimates the square roots of numbers <br> - Uses expressions with absolute value to represent situations <br> - Computes and interprets distance, given a set of ordered pairs (horizontal and vertical lines) | - Simplifies expressions containing square roots <br> - Uses expressions with absolute value to represent situations <br> - Simplifies radical expressions |  |
| New Vocabulary: feet per second, least common multiple | New Vocabulary: None | New Vocabulary: None |
| New Signs and Symbols: LCM lowest common multiple, sec second, square root symbol | New Signs and Symbols: i square root of -1 | New Signs and Symbols: None |

## Explanatory Notes

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## DesCartes: A Continuum of Learning ${ }^{\circledR}$

## Mathematics

Goal: The Real and Complex Number Systems

| Skills and concepts to Enhance (73\% Probability*) 251-260 | Skills and Concepts to Develop (50\% Probability*) $>260$ |
| :---: | :---: |
| Ratios and Proportional Relationships | Ratios and Proportional Relationships |
| - Solves problems involving successive discounts <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) <br> - Solves problems involving complex percent discounts (e.g., finding percent discount, regular price) <br> - Uses dimensional analysis for unit conversions (time) | - Solves problems involving successive discounts <br> - Solves problems involving rate conversions (e.g., mi/hr to ft/sec) |
| Perform Operations | Perform Operations |
| - Uses the additive inverse property with rational numbers <br> - Uses factor and multiple concepts to solve difficult problems <br> - Performs operations on complex numbers and expresses the results in simplest form | - Performs operations on complex numbers and expresses the results in simplest form |
| Extend and Use Properties | Extend and Use Properties |
| - Simplifies expressions containing square roots <br> - Uses expressions with absolute value to represent situations <br> - Simplifies radical expressions |  |
| New Vocabulary: None | New Vocabulary: None |
| New Signs and Symbols: i square root of -1 | New Signs and Symbols: None |

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    appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.

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     appropriate RIT ranges. Blank cells indicate data are limited or unavailable for this range or document version.

